

Chapter 1: Introduction

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Outline

- What is a signal?
- What is a system?
- Overview of specific systems
- Classification of signals
- Basic operations on signals
- Elementary signals
- Systems viewed as interconnections of operations
- Properties of systems
- Noises
- Theme example
- Exploring concepts with MATLAB





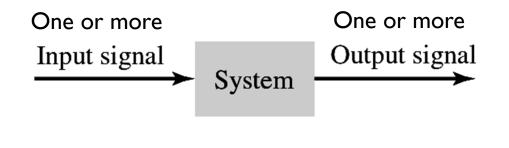
Introduction

What is a signal?

A signal is formally defined as a function of one or more variables that conveys information on the nature of a physical phenomenon.

What is a system?

• A system is formally defined as an entity that manipulates one or more signals to accomplish a function, thereby yielding new signals.







Overview of Specific Systems

Example I: Communication Systems



Figure 1.2: Elements of a communication system. The transmitter changes the message signal into a form suitable for transmission over the channel. The receiver processes the channel output (i.e., the received signal) to produce an estimate of the message signal.

- Analog communication systems
 - Modulator (AM, PM, FM) \rightarrow Channel \rightarrow Demodulator
- Digital communication systems
 - (Sampling+Quantization+Modulation+Coding) → Channel → (Reversed Function)
- Wireless/Wired Channel
 - Noise







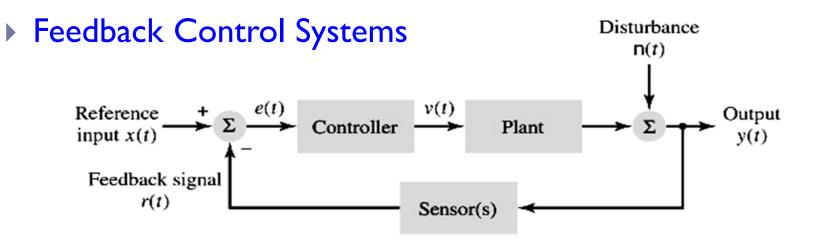


Figure 1.4 Block diagram of a feedback control system. The controller drives the plant, whose disturbed output drives the sensor(s). The resulting feedback signal is subtracted from the reference input to produce an error signal e(t), which, in turn, drives the controller.

- Response and Robustness
 - Single-input, single-output (SISO) system
 - Multiple-input, multiple-output (MIMO) system





Micro-electro-mechanical Systems (MEMS)

Merging mechanical systems with microelectronic control circuits on a silicon chip.

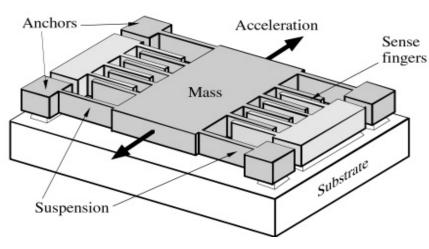
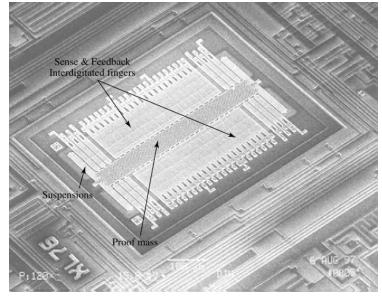


Figure 1.6 (Taken from Yazdi et al., *Proc. IEEE*, 1998) (a) Structure of lateral capacitive accelerometers.



(b) SEM view of Analog Device's ADXLO5 surface-micromachined polysilicon accelerometer.





Remote Sensing

- The process of acquiring information (detecting and measuring the changes) about an object of interest without being in physical contact with it
- Types of remote sensor
 - Radar sensor
 - Infrared sensor
 - Visible/near-infrared sensor
 - X-ray sensor



Figure 1.7 Perspectival view of Mount Shasta (California), derived from a pair of stereo radar images acquired from orbit with the Shuttle Imaging Radar. (Courtesy of Jet Propulsion Lab.)





Biomedical Signal Processing

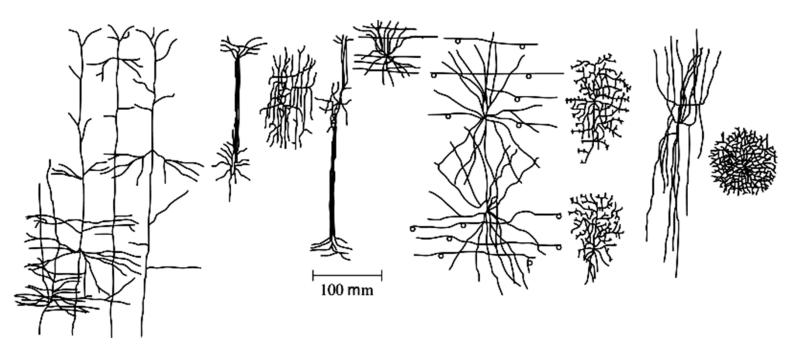


Figure 1.8 Morphological types of nerve cells (neurons) identifiable in monkey cerebral cortex, based on studies of primary somatic sensory and motor cortices. (Reproduced from E. R. Kande, J. H. Schwartz, and T. M. Jessel, *Principles of Neural Science*, 3d ed., 1991; courtesy of Appleton and Lange.)





Many biological signals (found in human body) is traced to the electrical activity of large groups of nerve cells or muscle cells

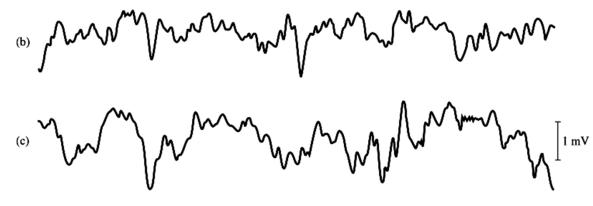


Figure 1.9 0s

The traces shown in (a), (b), and (c) are three examples of EEG signals recorded from the hippocampus of a rat. Neurobiological studies suggest that the hippocampus plays a key role in certain aspects of learning and memory.



2 s

Time —



SIGNAL BROCESSING

Specific System Example 6

Auditory System

• The three main parts of the ear

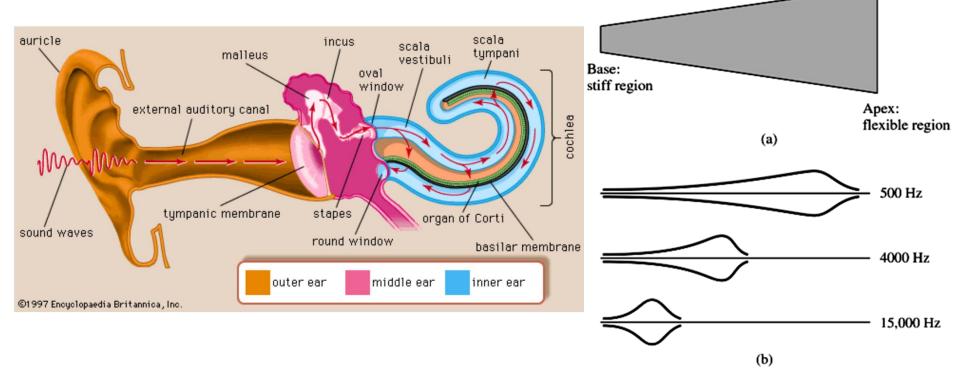


Figure 1.10

(a) In this diagram, the basilar membrane in the cochlea is depicted as if it were uncoiled and stretched out flat. (b) This diagram illustrates the traveling waves along the basilar membrane. 10 VLSI

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Overview of Specific Systems

- Analog versus Digital Signal Processing
 - Continuous-time approach
 - Natural way
 - Analog circuit elements: resistors, capacitors, inductors, AP, and diodes
 - Discrete-time approach
 - More complex and artificial way
 - □ Sampling (ADC) and Reconstruction (DAC)
 - Digital circuit elements: adder, shifter, multiplier, and memory
 - Flexibility
 - Repeatability

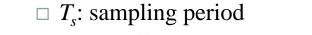


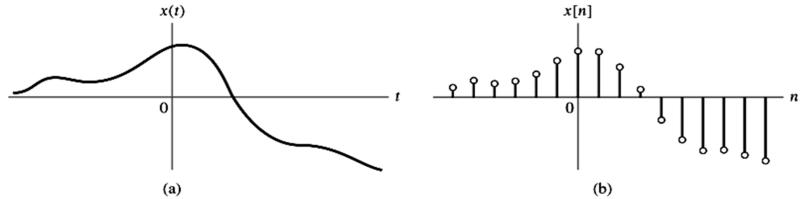




- We restrict our attention to one-dimensional signals only
 - I. Continuous-time and discrete-time signals
 - Continuous-time signals:
 - \square Real-valued or complex-valued function of time: x(t)
 - Discrete-time signals:

□ A time series: $\{x[n] = x(nT_s), n = 0, \pm 1, \pm 2, ...\}$







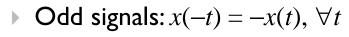
(a) Continuous-time signal x(t). (b) Representation of x(t) as a discrete-time signal x[n].

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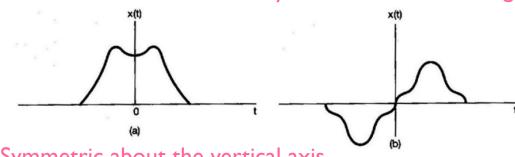




- 2. Even and odd signals
- For real-valued, continuous (or discrete) signal
 - Even signals: $x(-t) = x(t), \forall t$



Symmetric about the origin



Symmetric about the vertical axis

Example 1.1: Even or odd signal?

$$x(t) = \begin{cases} \sin\left(\frac{\pi t}{T}\right), & -T \le t \le T \\ 0, & \text{otherwise} \end{cases}$$





Even-Odd Decomposition of Signals

- An arbitrary signal $x(t) = x_e(t) + x_o(t)$ where $x_e(-t) = x_e(t)$ $x(-t) = x_e(-t) + x_o(-t)$ $x_o(-t) = -x_o(t)$ $= x_e(t) - x_o(t)$ $x_e = \frac{1}{2} [x(t) + x(-t)]$ (1.4) $x_o = \frac{1}{2} [x(t) - x(-t)]$ (1.5)
- Example 1.2
 - Even-odd decomposition of $x(t) = e^{-2t} \cos t$ Even component: $x_e(t) = \frac{1}{2}(e^{-2t}\cos t + e^{2t}\cos t)$ Odd component: $x_e(t) = \frac{1}{2}(e^{-2t}\cos t + e^{2t}\cos t)$ $x_o(t) = \frac{1}{2}(e^{-2t}\cos t e^{2t}\cos t)$ $= \cosh(2t)\cos t$ $= -\sinh(2t)\cos t$





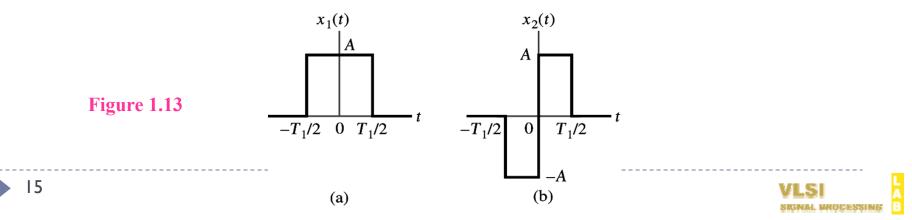
Conjugate Symmetric Complex Signals

A complex-valued signal x(t) is conjugate symmetric if its real part is even and its imaginary part is odd.

Proof:

Let x(t) = a(t) + jb(t) $x^{*}(t) = a(t) - jb(t)$ a(-t) + jb(-t) = a(t) - jb(t) a(-t) = a(t)b(-t) = -b(t)

- Example 1.2
 - A conjugate symmetric signal, where its real part is depicted in Fig. 1.13(a) and the imaginary part is in Fig. 1.13(b)





- ▶ 3. Periodic and nonperiodic signals
 - ▶ Periodic continuous-time signal: x(t+T) = x(t), $\forall t$
 - □ Clearly, $T=T_0$, $2T_0$, $3T_0$, Then, T_0 is called fundamental period and $2T_0$, $3T_0$, are harmonic
 - $\Box \text{ The reciprocal of the fundamental frequency is called frequency } f = \frac{1}{T_0}$

 \Box And, the angular frequency is defined by $\omega = 2\pi f$

- Nonperiodic signal: There is no finite T such that $x(t+T) = x(t), \forall t$
- Example: (a) periodic and (b) nonperiodic continuous-time signals

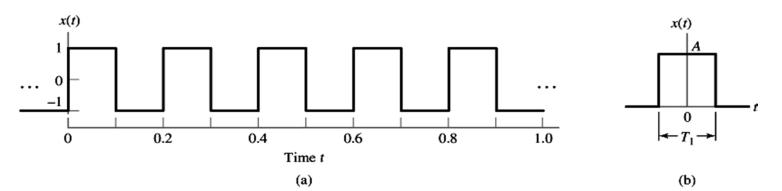


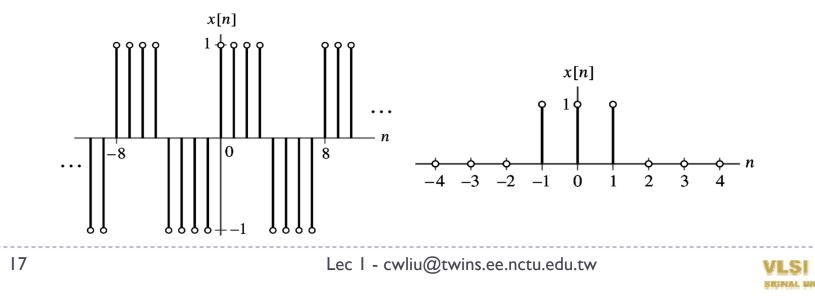
Figure 1.14 (a) Square wave with amplitude A = 1 and period T = 0.2s. (b) Rectangular pulse of amplitude A and duration T_1 .

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- ▶ 3. Periodic and nonperiodic signals
 - > Periodic discrete-time signal: x[n+N] = x[n], for integer *n*
 - \Box N is a positive integer
 - \Box The smallest integer N is called the fundamental period of x[n]
 - $\hfill\square$ The fundamental angular frequency is defined by $\Omega=2\pi/N$
 - Nonperiodic signal: There is no finite N such that x[n+N] = x[n], for integer n
 - Example: periodic and nonperiodic discrete-time signals





- 4. Deterministic signals and random signals
 - A deterministic signal is a signal about which there is no uncertainty with respect to its value at any time.
 - \Box sin(t), cos(t), ...
 - A random signal is a signal about which there is uncertainty before it occurs.

 $\hfill\square$ noise, stock price index, \ldots

- ▶ 5. Energy signals and power signals
 - The total energy of the continuous-time signal x(t) is defined by

$$E = \lim_{T \to \infty} \int_{\frac{-T}{2}}^{\frac{T}{2}} x^2(t) dt = \int_{-\infty}^{\infty} x^2(t) dt \quad (1.15)$$

> The power of the signal x(t) is defined by the time-averaged of (1.15)

$$P = \lim_{T \to \infty} \frac{1}{T} \int_{\frac{-T}{2}}^{\frac{T}{2}} x^2(t) dt \quad (1.16) \quad \text{or} \quad P = \frac{1}{T} \int_{\frac{-T}{2}}^{\frac{T}{2}} x^2(t) dt \quad (1.17)$$





Energy Signals and Power Signals

For discrete-time signal x[n], (1.15)–(1.17) become to

$$E = \sum_{n=-\infty}^{\infty} x^{2}[n] \quad (1.18) \quad P = \lim_{n \to \infty} \frac{1}{2N} \sum_{n=-N}^{N} x^{2}[n] \quad (1.19) \quad P = \frac{1}{N} \sum_{n=0}^{N-1} x^{2}[n] \quad (1.20)$$

- Energy signals: iff (if and only if) $0 < E < \infty$
- Power signals: iff $0 < P < \infty$
- The energy and power classifications of signals are mutually exclusive
- An energy signal has zero time-averaged power
- A power signal has infinite energy
- The periodic signals and random signals are usually power signals
- The deterministic, nonperiodic signals are usually energy signals





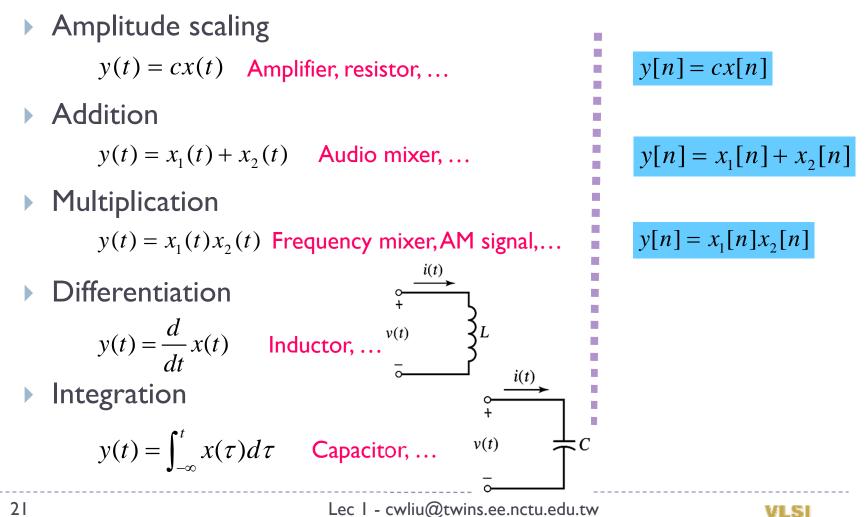
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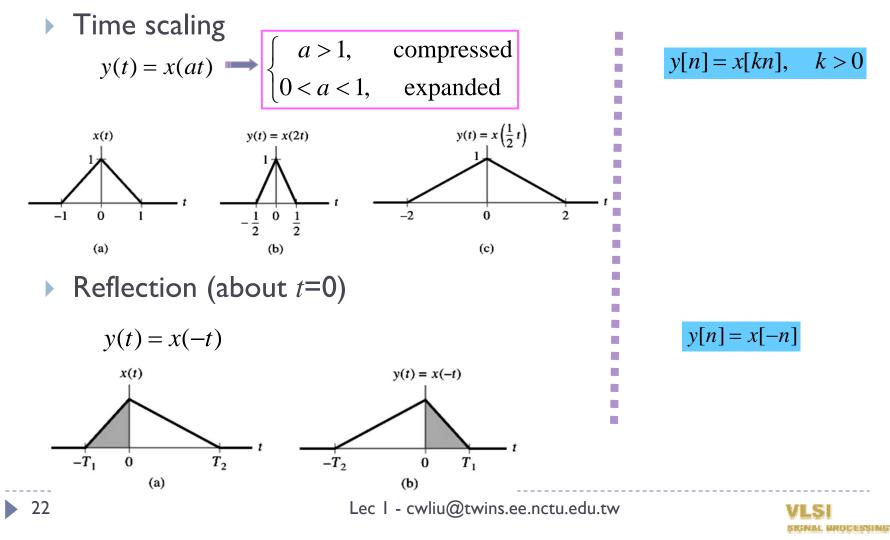


Operations performed on dependent variables

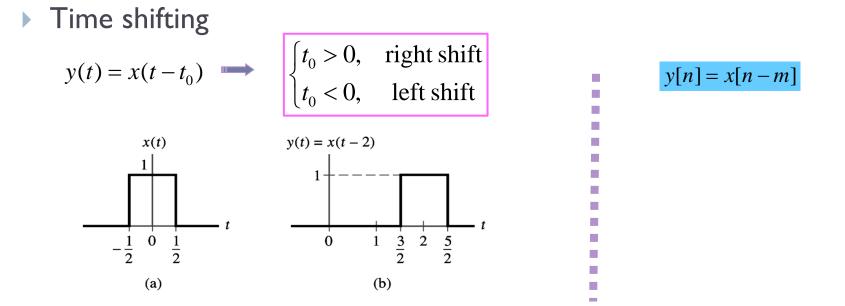




Operations performed on the independent variable













Precedence rule for time shifting and time scaling

• A combination of time shifting and time scaling operations

$$y(t) = x(at - b)$$

- > The operations must be performed in the correct order
 - The scaling operation always replaces t by at
 - The shifting operation always replaces t by t-b

time-shifting operation is performed first

$$v(t) = x(t-b)$$

y(t) = v(at) = x(at - b)

Example 1.5 y(t) = x(2t+3)v(t) = x(t + 3)y(t) = v(2t)y(0) = x(3) $y(\frac{-3}{2}) = x(0)$ -4 -3 -2 -1 0 -3 -2 -1 0 -1 0 (a) (b) (c) x(t)x(2t)y(*t*) $x(2t+3) \neq x(2(t+3))$ 24 -1 0 1 -3 -2 -1 00 1 (a) (c) (b)



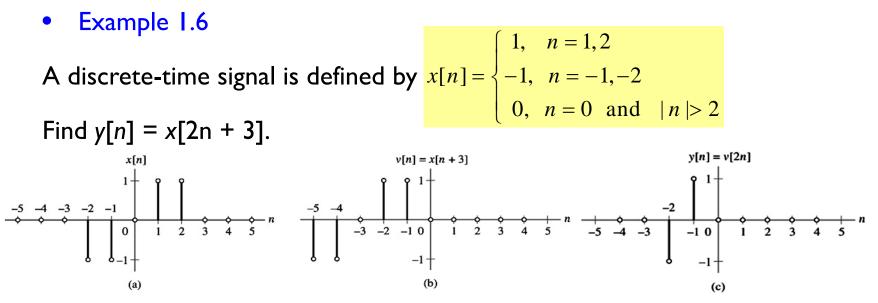


Figure 1.27

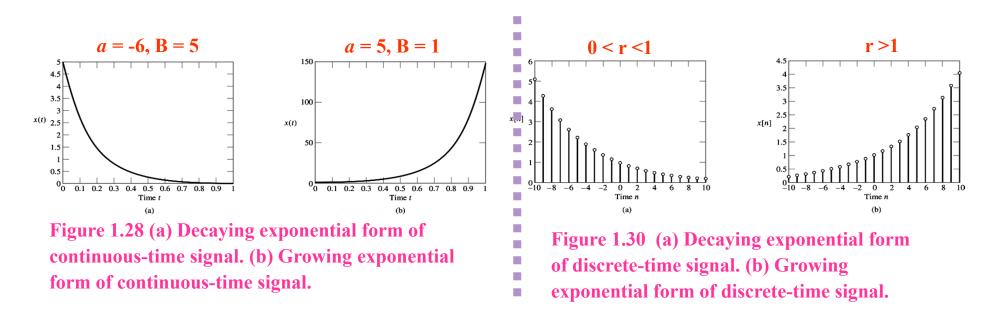
The proper order of applying the operations of time scaling and time shifting for the case of a discretetime signal. (a) Discrete-time signal x[n], antisymmetric about the origin. (b) Intermediate signal v(n) obtained by shifting x[n] to the left by 3 samples. (c) Discrete-time signal y[n] resulting from the compression of v[n] by a factor of 2, as a result of which two samples of the original x[n], located at n = -2, +2, are lost.





Elementary Signals

- ▶ I. Exponential Signals $x(t) = Be^{at}$ $x[n] = Br^n$
 - B and a can be real or complex parameters
 - Decaying exponential, if a < 0; growing exponential, if a > 0
 - > Decaying exponential, if 0 < r < 1; growing exponential, if r > 1

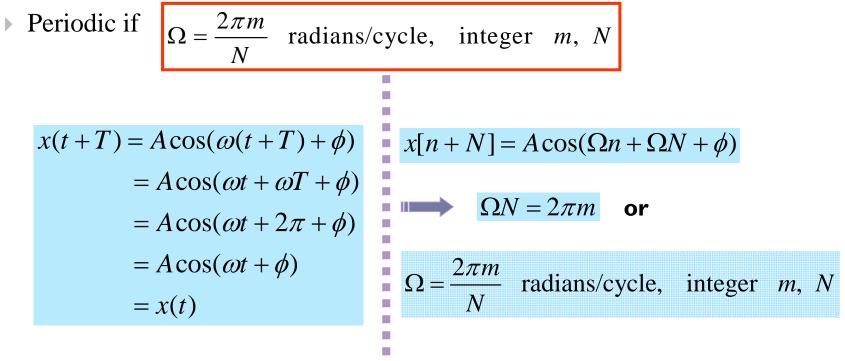






Elementary Signals

- ► 2. Sinusoidal Signals $x(t) = A\cos(\omega t + \phi)$ $x[n] = A\cos(\Omega n + \phi)$
 - Periodic continuous-time sinusoidal signals with period $T = 2\pi/\omega$
 - Discrete-time sinusoidal signals may or may not be periodic







Physical Examples

Ex.1 – exponential signals

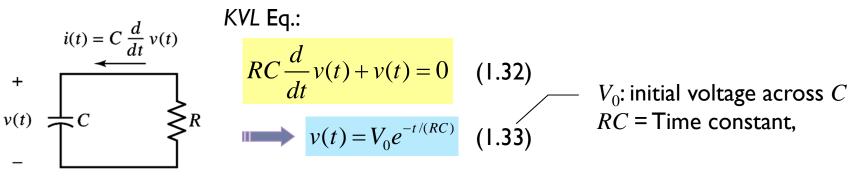


Figure 1.29 Lossy capacitor, with the loss represented by shunt resistance R.

Ex.2 – sinusoidal signals

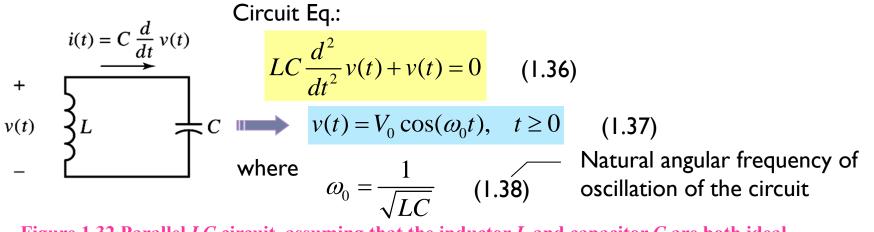


Figure 1.32 Parallel *LC* circuit, assuming that the inductor *L* and capacitor *C* are both ideal.

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Example 1.7 Discrete-Time Sinusoida (Construction) Signals

- A pair of sinusoidal signals with a common angular frequency is defined by $x_1[n] = \sin[5\pi n], x_2[n] = \sqrt{3}\cos[5\pi n]$
 - (a) Both signals are periodic. Find their common fundamental period.
 - (b) Express the composite sinusoidal signal $y[n]=x_1[n]+x_2[n]$ in the form $y[n] = A\cos(\Omega n + \phi)$

Sol.
(a)
$$\Omega = 5\pi$$
 radians/cycle $N = \frac{2\pi m}{\Omega} = \frac{2\pi m}{5\pi} = \frac{2m}{5}$

This can be only for $m = 5, 10, 15, \ldots$, which results in $N = 2, 4, 6, \ldots$

(b)
$$A\cos(\Omega n + \phi) = A\cos(\Omega n)\cos(\phi) - A\sin(\Omega n)\sin(\phi)$$

 $A\sin(\phi) = -1$ and $A\cos(\phi) = \sqrt{3}$

 $y[n] = 2\cos(n)$

Solve
$$\phi$$
 and A
 $\tan(\phi) = \frac{\sin(\phi)}{\cos(\phi)} = \frac{\text{amplitude of } x_1[n]}{\text{amplitude of } x_2[n]} = \frac{-1}{\sqrt{3}}$

$$\phi = -\pi/6$$

$$A = \frac{-1}{\sin(-\pi/6)} = 2$$
Hence, we have

VLSI SIGNAL PROCESSING



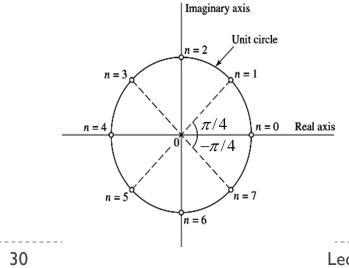
Euler's Identity

• 3. Relation Between Sinusoidal and Complex Exponential Signals

• Euler's identity: $e^{j\theta} = \cos\theta + j\sin\theta$

$$Be^{j\omega t}$$

= $Ae^{j\phi}e^{j\omega t}$
= $Ae^{j(\phi+\omega t)}$
= $A\cos(\omega t + \phi) + jA\sin(\omega t + \phi)$



$$A\cos(\omega t + \phi) = \operatorname{Re}\{Be^{j\omega t}\}\$$
$$A\sin(\omega t + \phi) = \operatorname{Im}\{Be^{j\omega t}\}\$$

$$A\sin(\Omega n + \phi) = \operatorname{Im} \{Be^{j\Omega n}\}\$$
$$A\cos(\Omega n + \phi) = \operatorname{Re} \{Be^{j\Omega n}\}\$$

Figure 1.34 Complex plane, showing eight points uniformly distributed on the unit circle. The projection of the points on the real axis is $cos(n\pi/4)$, while the projection on the imaginary axis is $sin(n\pi/4)$; n=0,1, ..., 7.

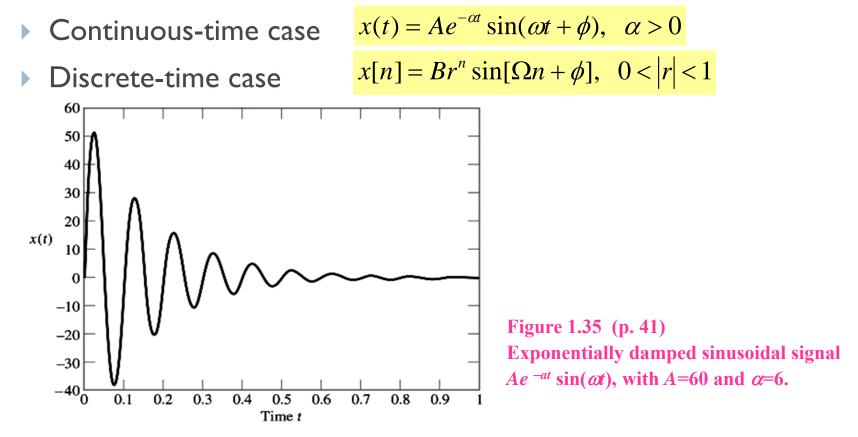
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Elementary Signals

▶ 4. Exponential Damped Sinusoidal Signals





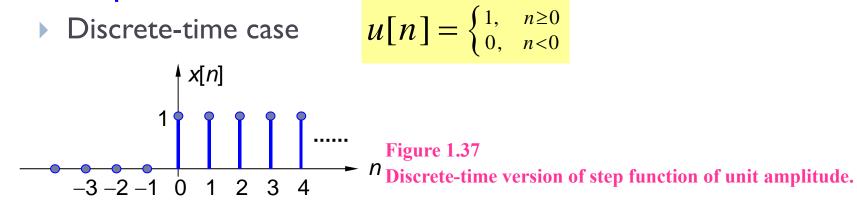


Elementary Signals

▶ 5. Step Function

T

0



• Continuous-time case
$$u(t) = \begin{cases} 1, & t > 0 \\ 0, & t < 0 \end{cases}$$

t

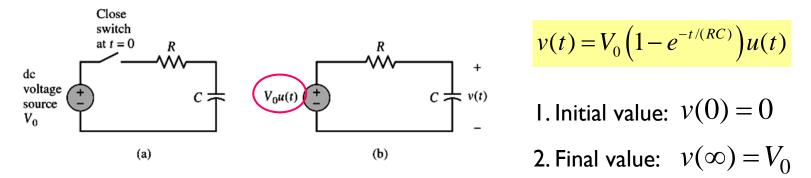
Figure 1.38 Continuous-time version of the unit-step function of unit amplitude.



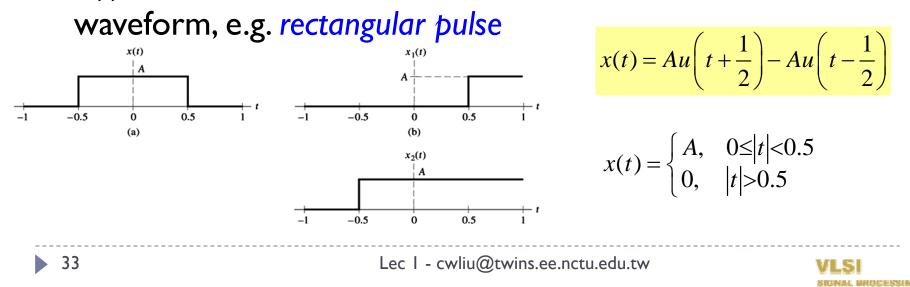


Unit-Step Function Application

• u(t) is a particularly simple signal to apply



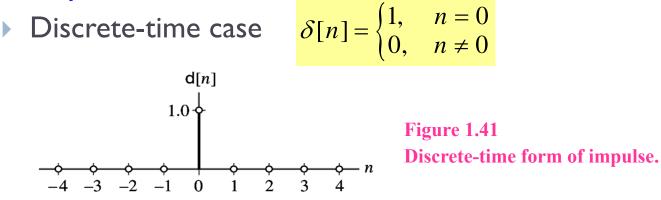
• u(t) can be used to construct other discontinuous



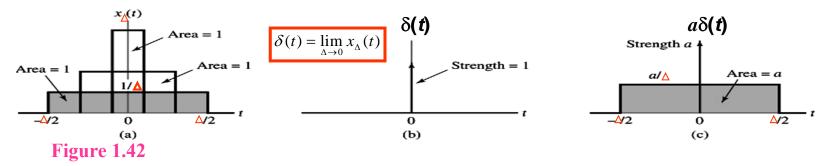


Elementary Signals

▶ 6. Impulse Function



• Continuous-time case $\delta(t) = 0$ for $t \neq 0$ and $\int_{-\infty}^{\infty} \delta(t) dt = 1$



- (a) Evolution of a rectangular pulse of unit area into an impulse of unit strength.
- (b) Graphical symbol for unit impulse. (c) Representation of an impulse of strength *a*.



Impulse Function

- AKA Dirac delta function
 - $\delta(t)$ is zero everywhere except at the origin
 - The total area under the impulse $\delta(t)$ (or unit impulse), called the strength, is unity
- Mathematical relation between impulse and rectangular functions:

- $\delta(t) = \lim_{\Delta \to 0} x_{\Delta}(t)$ 1. $x_{\Delta}(t)$: even function of t, Δ = duration. 2. $x_{\Lambda}(t)$: Unit area.
- $\delta(t)$ is the derivative of u(t); u(t) is the integral of $\delta(t)$:

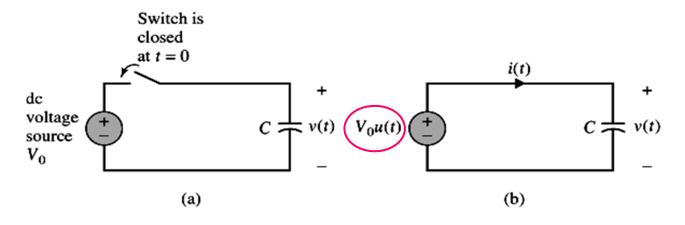
$$\delta(t) = \frac{d}{dt}u(t) \quad (1.62)$$

$$u(t) = \int_{-\infty}^{t} \delta(\tau) d\tau$$
 (1.63)





RC Circuit Example (conti.)



I.Voltage across the capacitor:

 $v(t) = V_0 u(t)$

2. Current flowing through capacitor:

$$i(t) = C \frac{dv(t)}{dt} \longrightarrow i(t) = CV_0 \frac{du(t)}{dt} = CV_0 \delta(t)$$





Properties of $\delta(t)$

- Even function
- Shifting property

 $\delta(-t) = \delta(t)$ $\int_{-\infty}^{\infty} x(t)\delta(t-t_0)dt = x(t_0)$ If x(t) is continuous at t_0

• Time-scaling property $\delta(at) = \frac{1}{\delta}\delta(t), \quad a > 0$

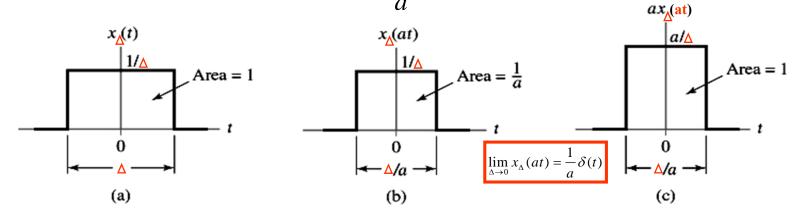


Figure 1.44 Steps involved in proving the time-scaling property of the unit impulse. (a) Rectangular pulse $x\Delta(t)$ of amplitude $1/\Delta$ and duration Δ , symmetric about the origin. (b) Pulse $x\Delta(t)$ compressed by factor *a*. (c) Amplitude scaling of the compressed pulse, restoring it to unit area.



Elementary Signals

7. Derivation of the Impulse

► Doublet $\delta^{(1)}(t)$: the first derivative of $\delta(t)$ ► Recall Example I.8, the rectangular pulse is $x(t) = Au\left(t + \frac{1}{2}\right) - Au\left(t - \frac{1}{2}\right)$ → Unit rectangular pulse is equal to $\frac{1}{\Delta}(u(t + \frac{\Delta}{2}) - u(t - \frac{\Delta}{2}))$

$$\delta^{(1)}(t) = \lim_{\Delta \to 0} \frac{1}{\Delta} \left(\delta(t + \Delta/2) - \delta(t - \Delta/2) \right)$$

Fundamental property of the doublet

$$\int_{-\infty}^{\infty} f(t)\delta^{(1)}(t-t_0)dt = \frac{d}{dt}f(t)\Big|_{t=t_0} \qquad \int_{-\infty}^{\infty}\delta^{(1)}(t)dt = 0$$

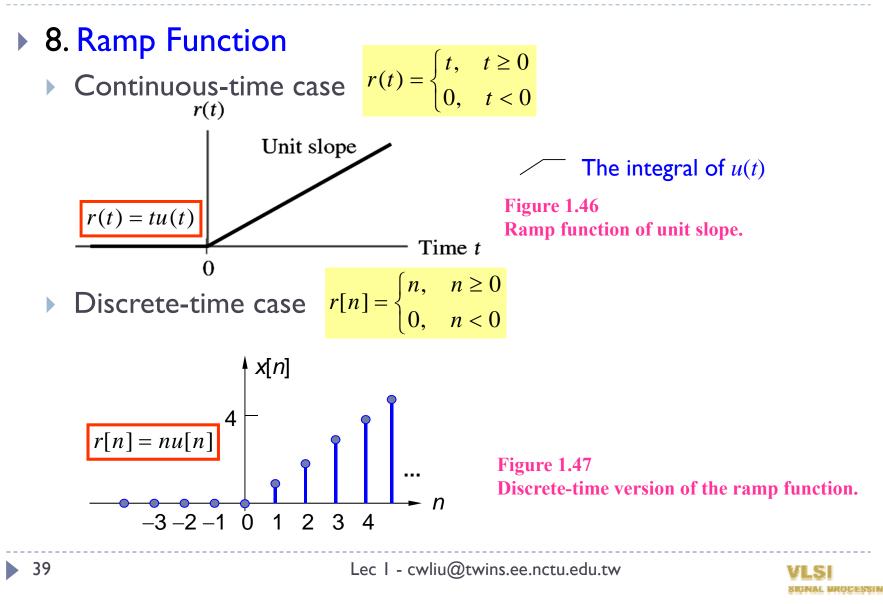
Second derivative of impulse

$$\frac{\partial^2}{\partial t^2}\delta(t) = \frac{d}{dt}\delta^{(1)}(t) = \lim_{\Delta \to 0}\frac{\delta^{(1)}(t + \Delta/2) - \delta^{(1)}(t - \Delta/2)}{\Delta}$$





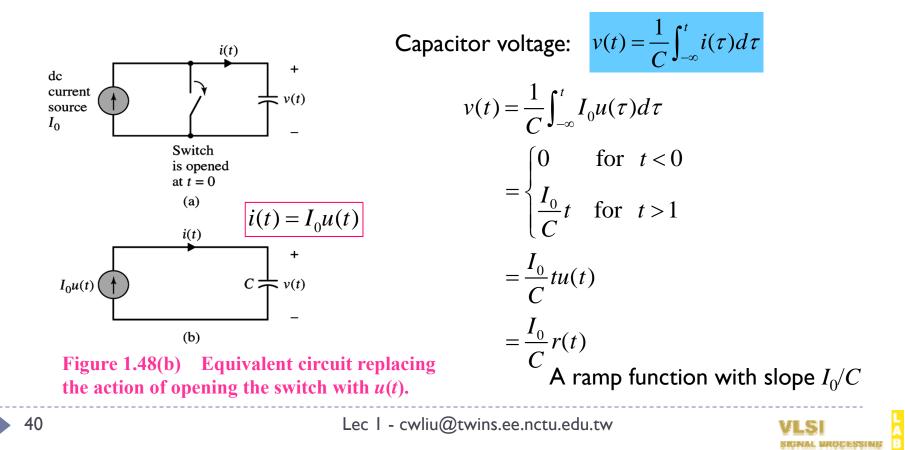
Elementary Functions





Example 1.11 Parallel Circuit

Consider the parallel circuit of Fig. 1-48 (a) involving a dc current source I_0 and an initially uncharged capacitor C. The switch across the capacitor is suddenly opened at time t = 0. Determine the current *i*(*t*) flowing through the capacitor and the voltage *v*(*t*) across it for t \ge 0.





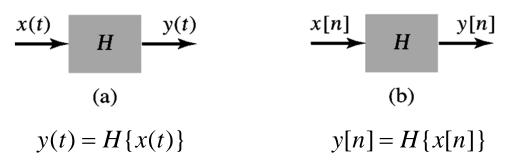
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Systems Viewed as Interconnection

- A system is an interconnection of operations that transforms an input signal into an output signal
 - Let the operator $H\{\cdot\}$ denote the overall action of a system



• Example: Discrete-time shift operator *S*^{*k*}:

$$x[n] \longrightarrow S^{k} \xrightarrow{x[n-k]}$$

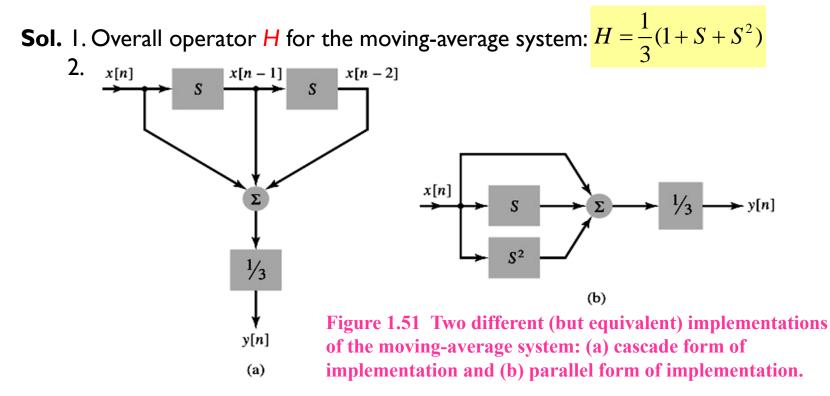
$$\longrightarrow Shifts the input by k time units$$

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Example 1.12 Moving-Average System

Consider a discrete-time system whose output signal y[n] is the average of three most recent values of the input signal x[n], i.e. $y[n] = \frac{1}{3}(x[n] + x[n-1] + x[n-2])$ Formulate the operator *H* for this system; hence, develop a block diagram representation for it.







► I. Stability

- A system is said to be bounded-input, bounded-output (BIBO) stable iff every bounded input results in a bounded output.
- The operator *H* is *BIBO* stable if

$$|y(t)| \le M_y < \infty \quad \forall t$$
, whenever $|x(t)| \le M_x < \infty \quad \forall t$.

Example 1.13

Finite moving-average system is BIBO stable

$$|y[n]| = \frac{1}{3} |x[n] + x[n-1] + x[n-2]|$$

$$\leq \frac{1}{3} (|x[n]| + |x[n-1]| + |x[n-2]|)$$

$$\leq \frac{1}{3} (M_x + M_x + M_x)$$

$$= M_x$$





> 2. Memory

A system is said to possess *memory* if its output signal depends on past or future values of the input signal.

• Inductor
$$i(t) = \frac{1}{L} \int_{-\infty}^{t} v(\tau) d\tau$$
 Depends on the infinite past voltage

• Moving-average system
$$y[n] = \frac{1}{3}(x[n] + x[n-1] + x[n-2])$$

Depends on two past values of x[n]

- A system is said to possess memoryless if its output signal depends only on the present values of the input signal.
 - Resistor $i(t) = \frac{1}{R}v(t)$

• A square-law system $y[n] = x^2[n]$





► 3. Causality

- Causality is required for a system to be capable of operating in real time.
- A system is said to be *causal* if its output signal depends only on the present or past values of the input signal.
- A system is said to be *noncausal* if its output signal depends on one or more future values of the input signal.
- For example,
 - Causal moving-average system, $y[n] = \frac{1}{3}(x[n] + x[n-1] + x[n-2])$

• Noncausal moving-average system, $y[n] = \frac{1}{3}(x[n+1] + x[n] + x[n-1])$





- 4. Invertibility
 - A system is said to be *invertible* if the input of the system can be recovered from the output.

$$\begin{array}{c} x(t) \\ \longrightarrow \\ H \\ \end{array} \\ H^{inv} \left\{ y(t) \right\} = H^{inv} \left\{ H\left\{ x(t) \right\} \right\} = H^{inv} H\left\{ x(t) \right\} \\ \end{array} \\ \begin{array}{c} \longrightarrow \\ H^{inv} H = I \end{array} \\ \end{array} \\ \begin{array}{c} \text{Condition for an invertible system} \end{array}$$

- H^{inv} : inverse operator; *I*: identity operator
- A one-to-one mapping between input and output signals for a system is invertible
 - Distinct inputs applied to the system produce distinct outputs.
- The inverse of the communication channel is aka the equalizer



Invertible and Noninvertible Systems of HERRONG (CONTROLLER OF HERRONG)

Example 1.15 – Inverse of System

Consider the time-shift system described by the input-output relation $y(t) = x(t - t_0) = S^{t_0} \{x(t)\}$, where the operator S^{t_0} represents a time shift of t_0 seconds. Find the inverse of this system.

 $S^{-t_0}\{y(t)\} = S^{-t_0}\{S^{t_0}\{x(t)\}\} = S^{-t_0}S^{t_0}\{x(t)\} \qquad S^{-t_0}S^{t_0} = I$

Example 1.16 – Non-Invertible System

Show that a square-law system described by the input-output relation

 $y(t) = x^2(t)$ is not invertible.

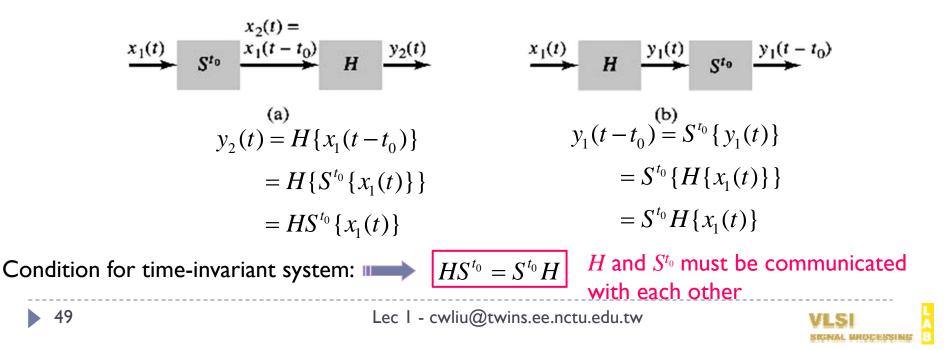
Since the distinct inputs x(t) and -x(t) produce the same output y(t). Not 1-1 mapping. Accordingly, the square-law system is not invertible.



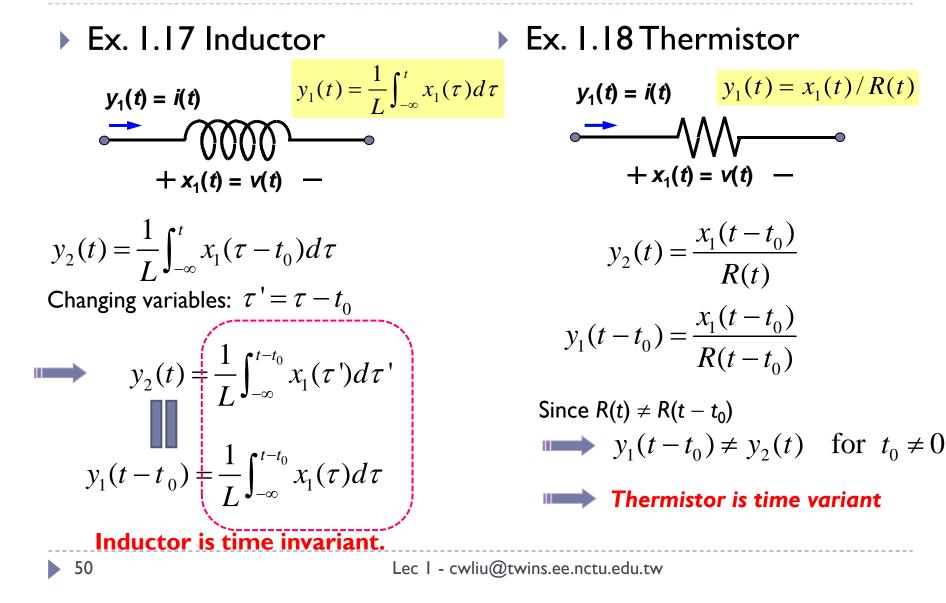


► 5.Time invariance

- A system is said to be time invariant if a time delay (or time advance) of the input signal leads to an identical time shift in the output signal.
 - A time-invariant system responds identically no matter when the input signal is applied.



Example 1.17 vs. Example 1.18





▶ 6. Linearity

Superposition property

 $H\{x_1(t)\} + H\{x_2(t)\} = y_1(t) + y_2(t) = H\{x_1(t) + x_2(t)\}$

Homogeneity property

 $aH\{x_1(t)\} = ay_1(t) = H\{ax_1(t)\}, a = \text{constant factor}$

A system is said to be *linear* if it satisfies the superposition and homogeneity properties

If $x(t) = \sum_{i=1}^{N} a_i x_i(t)$ (1.86) $x_1(t), x_2(t), \dots, x_N(t) \equiv \text{ input signal};$ $a_1, a_2, \dots, a_N \equiv \text{ Corresponding weighted factor}$

• then $y(t) = H\{x(t)\} = H\{\sum_{i=1}^{N} a_i x_i(t)\}$ linear $y(t) = \sum_{i=1}^{N} a_i y_i(t)$





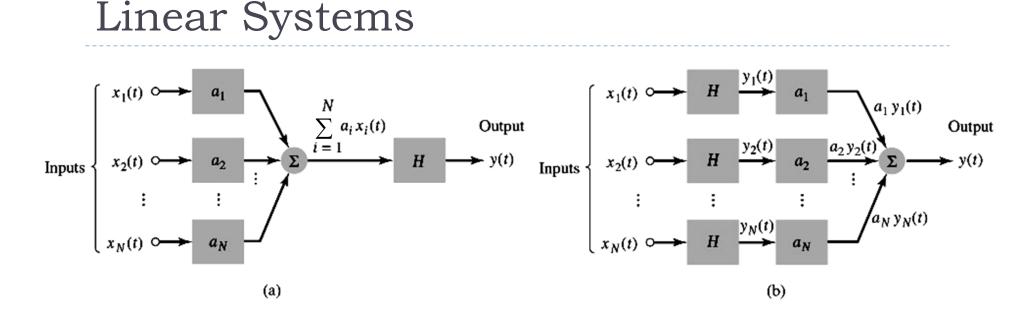


Figure 1.56 The linearity property of a system. (a) The combined operation of amplitude scaling and summation precedes the operator H for multiple inputs. (b) The operator H precedes amplitude scaling for each input; the resulting outputs are summed to produce the overall output y(t). If these two configurations produce the same output y(t), the operator H is linear.



Outline

- What is a signal?
- What is a system?
- Overview of specific systems
- Classification of signals
- Basic operations on signals
- Elementary signals
- Systems viewed as interconnections of operations
- Properties of systems
- Noises
- Theme example
- Exploring concepts with MATLAB

