

# Principles of Communications

## Lecture 7: Analog Modulation Techniques (5)

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# Outlines

- Linear Modulation
- Angle Modulation
- Interference
- Feedback Demodulators
- Analog Pulse Modulation
- Delta Modulation and PCM
- Multiplexing

# Analog Pulse Modulation

- Message waveform is represented by regularly spaced sample values (sample signals) – discrete in time.
- Historically, these methods are the early attempts to achieve modern communications. They are in the twilight zone between analog and digital modulations.
- Today, their basic forms can still be found in some electronic components such as ADC.

# Analog/Digital Pulse-coded

- ***Analog pulse modulation:*** A pulse train is used as the carrier wave. Some characteristic feature of each pulse (e.g., amplitude, duration, or position) is used to represent message samples.

PAM – pulse amplitude

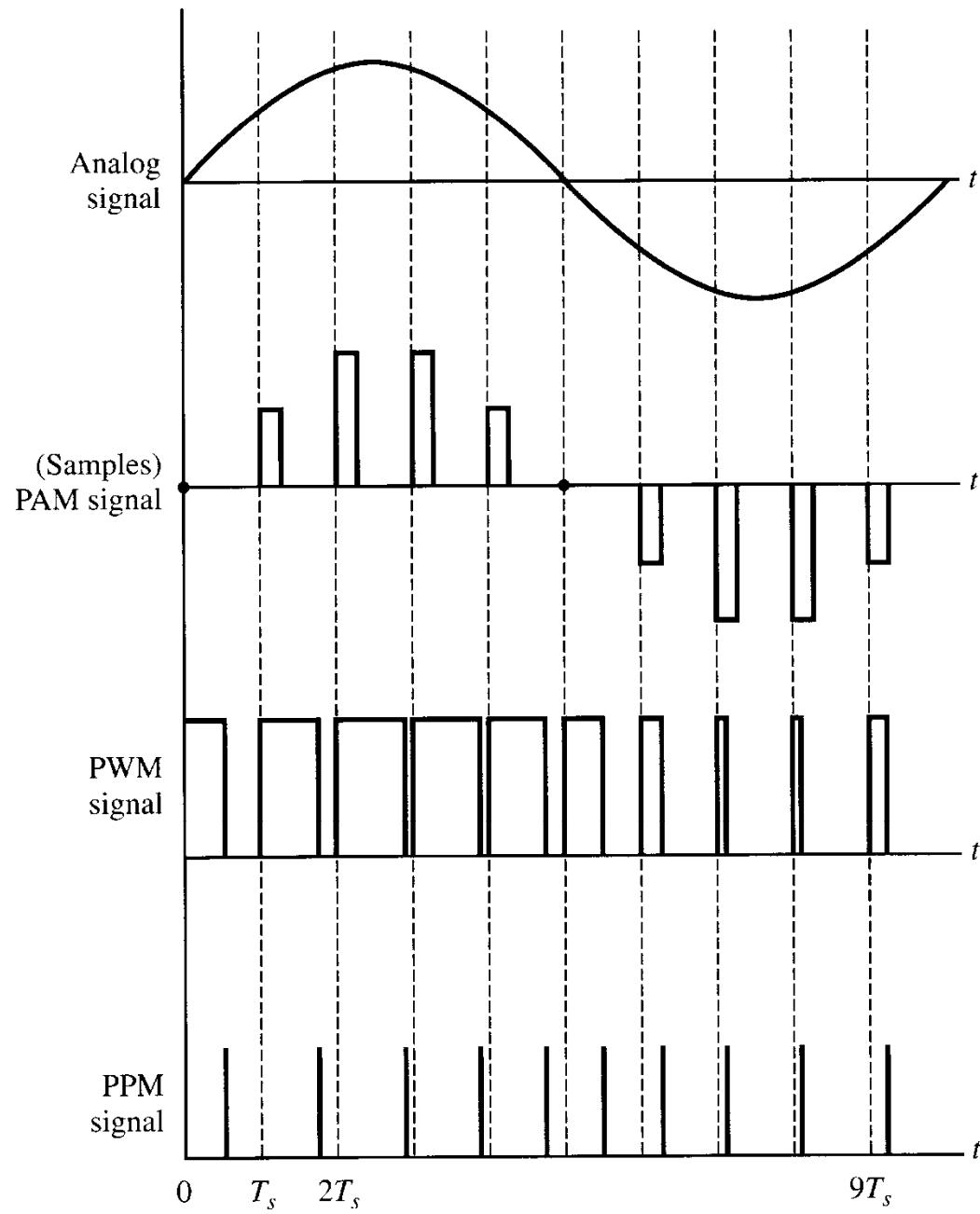
PDM – pulse duration

PPM – pulse position

- ***Digital Pulse Modulation:*** Messages are discrete-amplitude (finite levels) samples.

DM – delta modulation

PCM – pulse-code modulation



**Figure 3.56**  
Illustration of PAM, PWM, and PPM.

# Pulse-Amplitude Modulation (PAM)

- The amplitude of each pulse corresponds to the value of the message signal  $m(t)$  (at the leading edge of the pulse).

$$m_c(t) = \sum_{n=-\infty}^{\infty} m(nT_s) \cdot \Pi\left[\frac{t - (nT_s + 0.5\tau)}{\tau}\right]$$

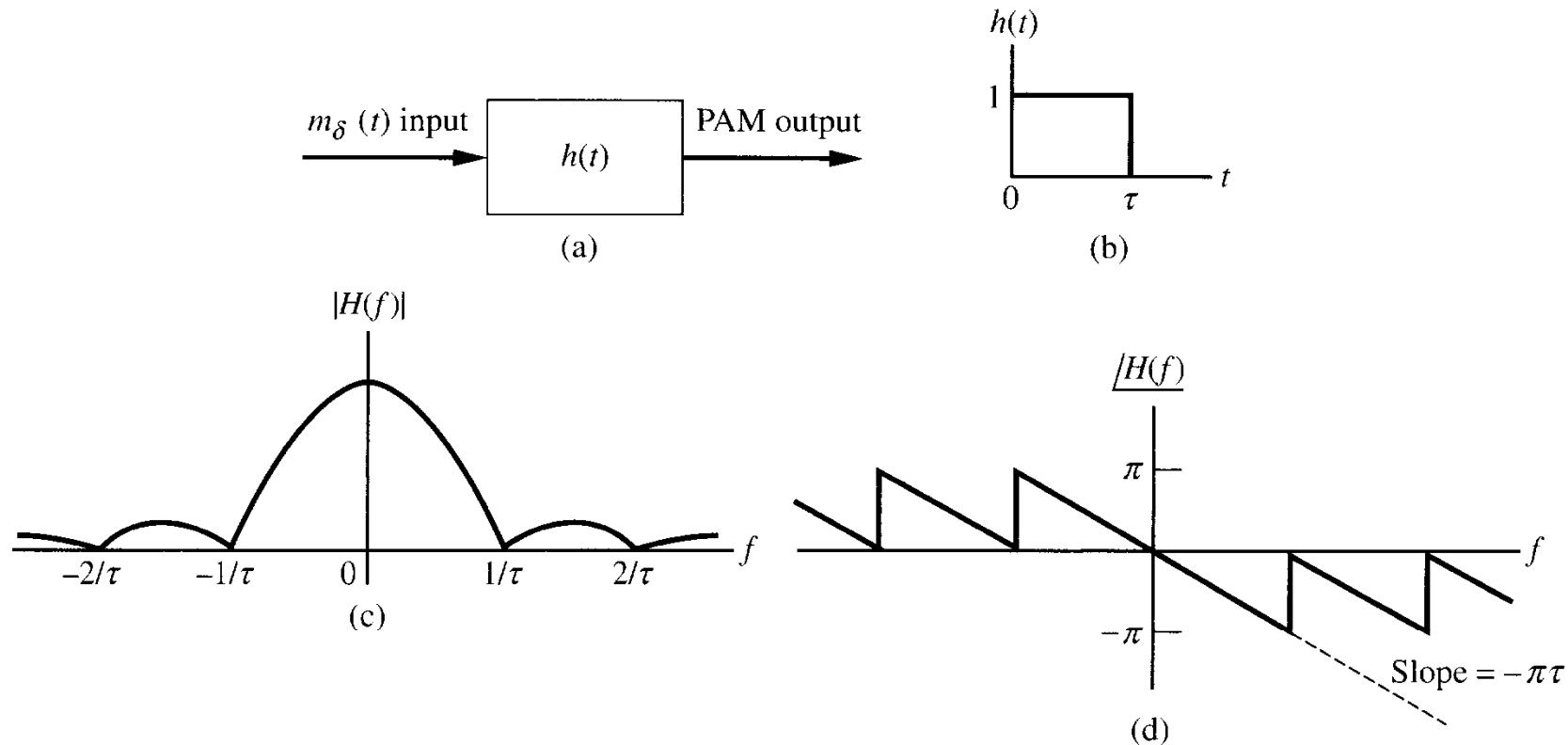
$$\text{where } \Pi\left(\frac{t}{W}\right) = \begin{cases} 1, & |t| < W/2 \\ 0, & \text{otherwise} \end{cases}$$

- The *pulse generator* can be considered as a “filter”.

$$\begin{cases} m_c(t) = m_\delta(t) * h(t), & h(t) = \Pi\left[\frac{t - 0.5\tau}{\tau}\right] \\ M_c(f) = M_\delta(f) \cdot H(f), & H(f) = \tau \cdot \text{sinc}f\tau \cdot e^{-j\pi f\tau} \end{cases}$$

$$m_\delta(t) = \sum_{n=-\infty}^{\infty} m(nT_s) \delta(t - nT_s) \quad \text{sampled message}$$

# PAM Signals



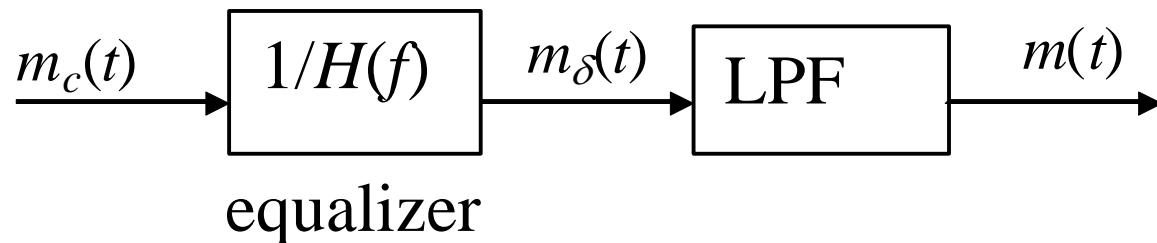
**Figure 3.57**

Generation of PAM. (a) Holding network. (b) Impulse response of holding network. (c) Amplitude response of holding network. (d) Phase response of holding network.

# Demodulation

- Recover  $M_\delta(f) \leftrightarrow m_\delta(t)$  samples
- Recover  $M(f) \leftrightarrow m(t)$  message

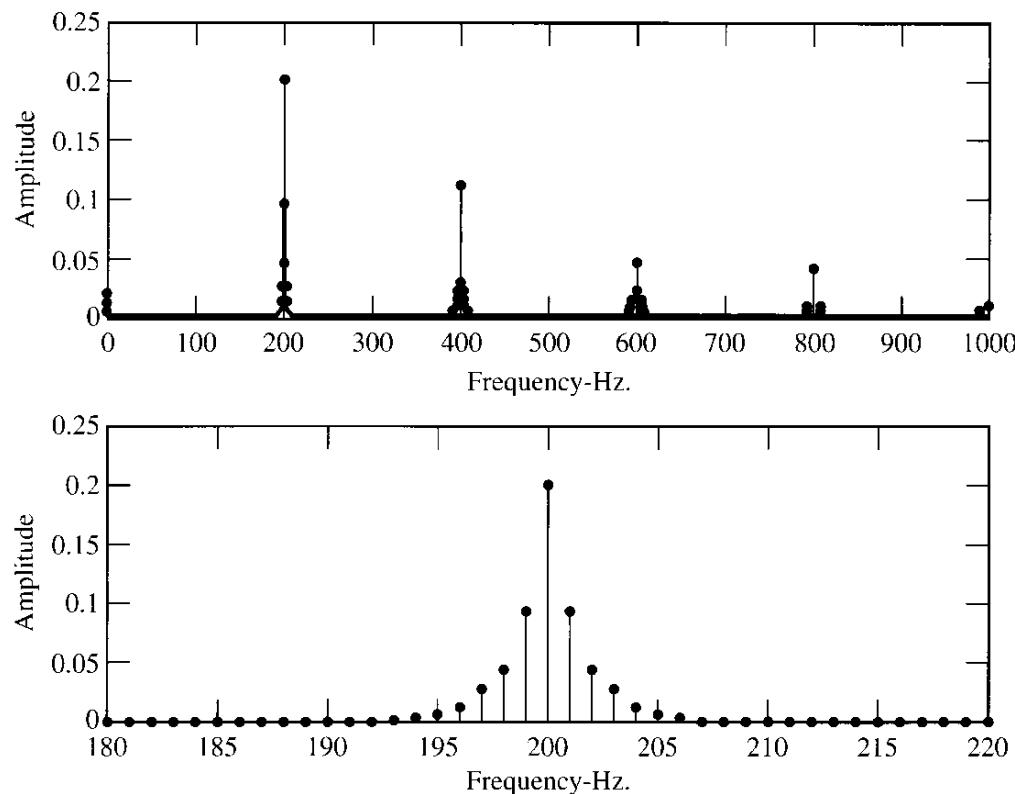
$$M_\delta(f) = \frac{M_c(f)}{H(f)}$$



- **Equalizer:** Recover distorted signals particularly when the distortion method is known or estimated.

# Pulse-Width Modulation (PWM)

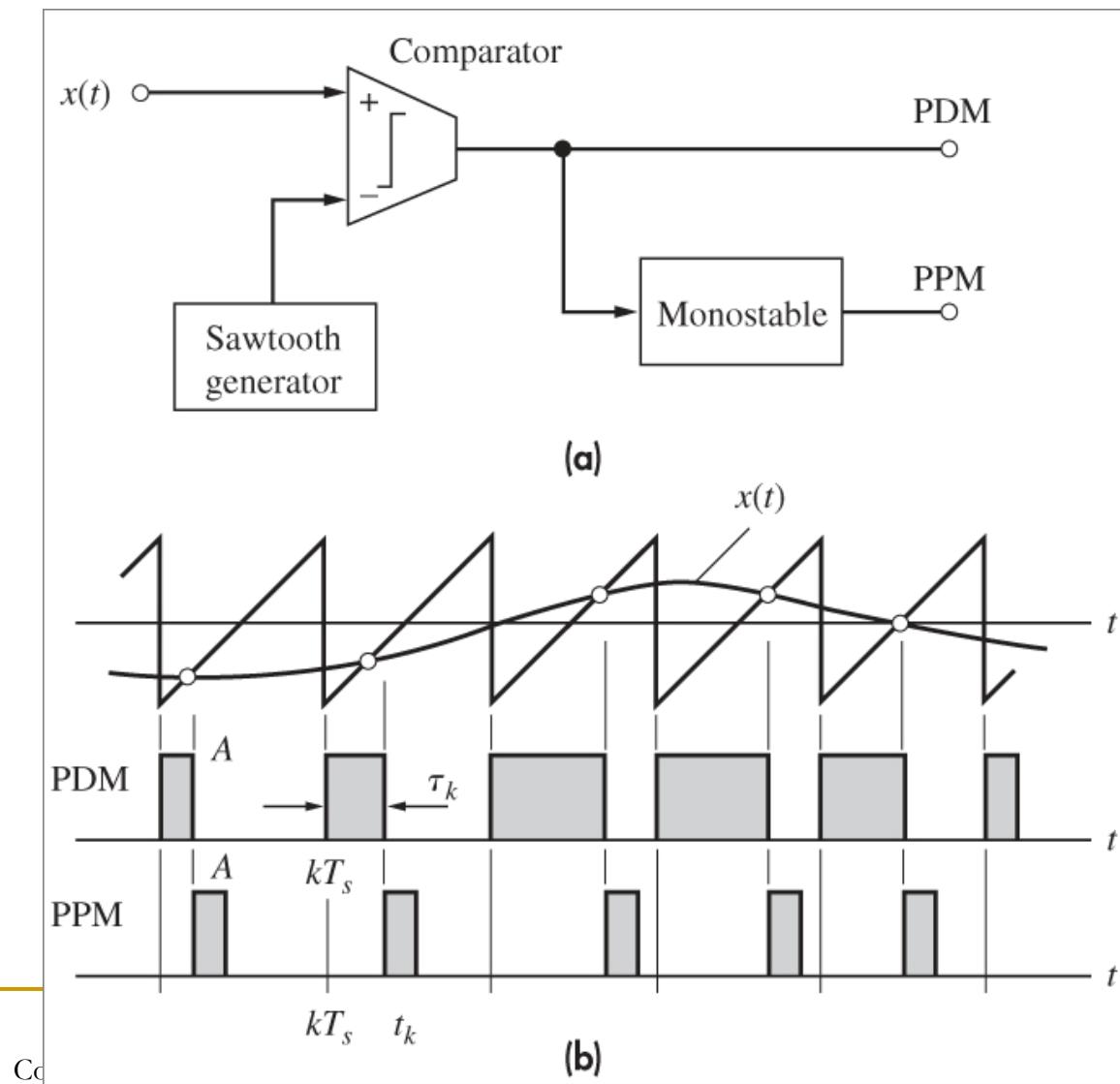
- Pulse width  $\propto$  the values of message
- Spectrum: complicated (Fourier-Bessel spectra)



**Figure 3.58**  
Spectrum of a PWM signal. (a) Spectrum for  $0 \leq f \leq 1000$  Hz. (b) Spectrum in the neighborhood of  $f = 200$  Hz.

# PWM/PPM Generation

- Mod: <Carlson, Fig.6-3-2>
  - Demod: area of “pulse”.
- Low-pass filtering  
(integration)



# Pulse-Position Modulation (PPM)

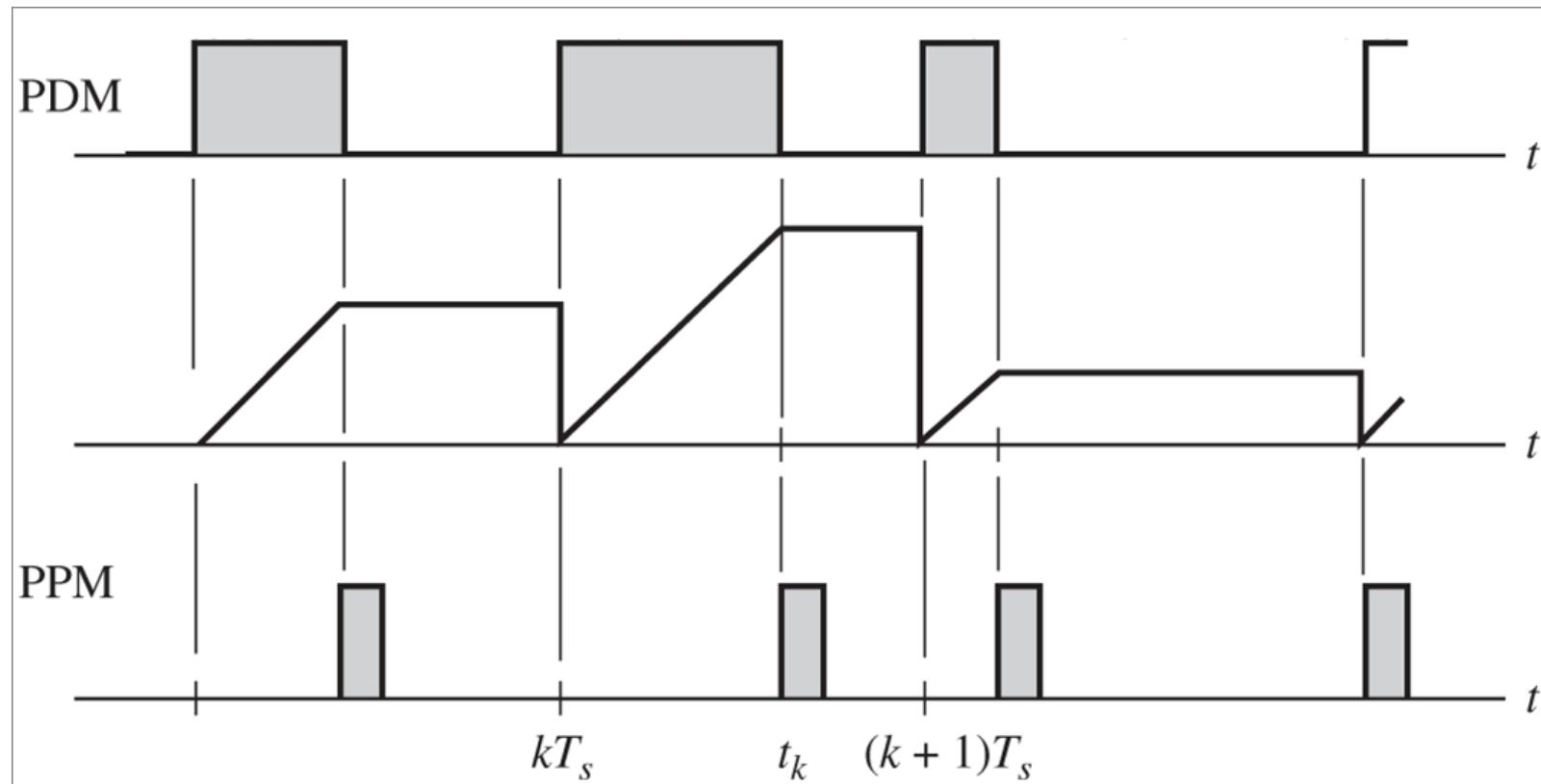
- Pulse position  $\propto$  the values of message

$$x(t) = \sum_{n=-\infty}^{\infty} g(t - t_n)$$

- Spectrum: complicated
- Demodulation: (1) LPF & integration  
(2) convert PPM to PWM  $\rightarrow$  LPF
- Conversion of PPM or PWM to PAM: a ramp generator  
(re)starts at  $kT_s$  and stops at  $t_k$ . (next page)

# Conversion Between PWM & PPM

<Carlson, Fig.6-3.3> (integration)



# Delta Modulation

- $m(t) \rightarrow$  samples (analog amplitude)  $\rightarrow$  difference  $\rightarrow$  binary  
or  $m(t) \rightarrow$  difference  $\rightarrow$  binary  $\rightarrow$  samples
- Operations:

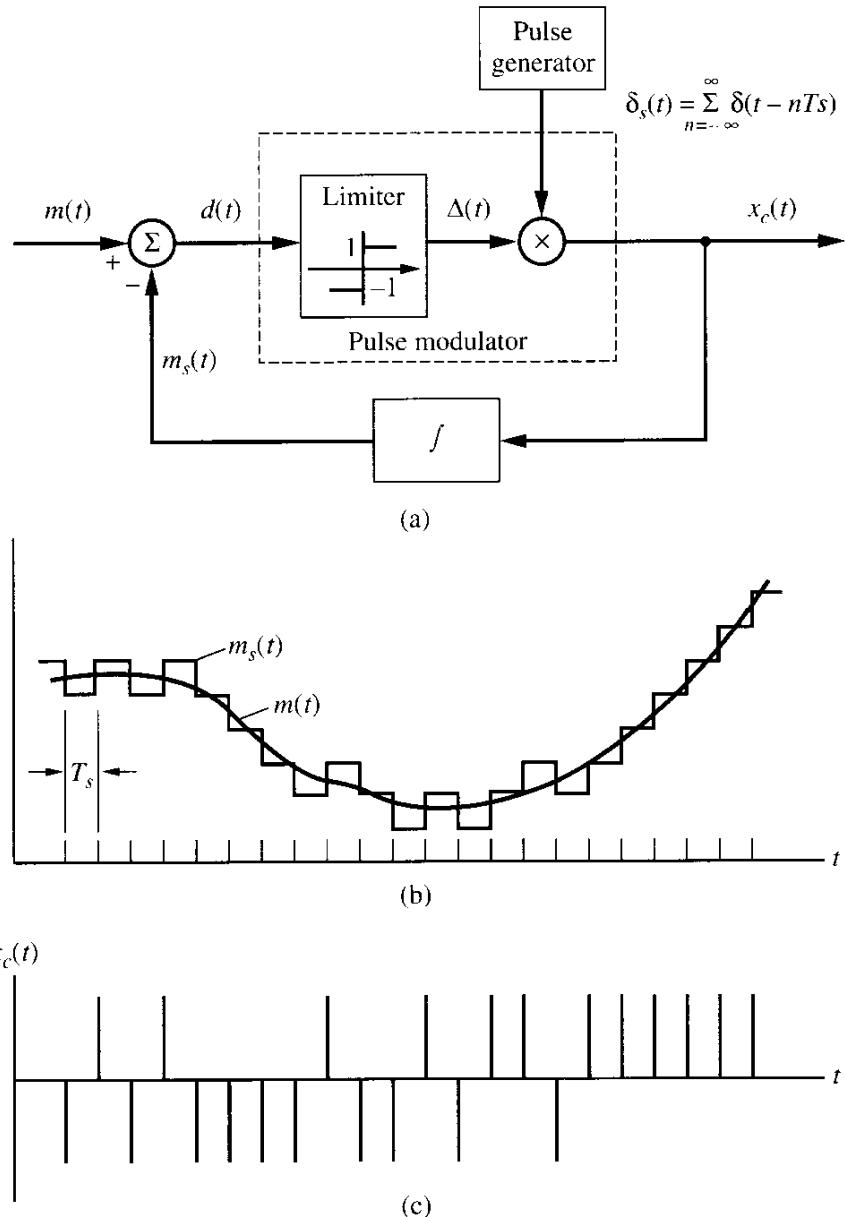
$$(1) \quad d(t) = m(t) - m_s(t)$$

$$(2) \quad \Delta(t) = \text{threshold}(d(t)) = \begin{cases} \delta_0, & d(t) \geq 0 \\ -\delta_0, & d(t) < 0 \end{cases}$$

$$(3) \quad x_c(t) = \text{samples of } \Delta(t) = \Delta(t) \cdot \sum_{n=-\infty}^{\infty} \delta(t - nT_s) = \sum_{n=-\infty}^{\infty} \Delta(nT_s) \delta(t - nT_s)$$

$$(4) \quad m_s(t) = \sum_{n=-\infty}^{\infty} \Delta(nT_s) \int_0^t \delta(\alpha - nT_s) d\alpha$$

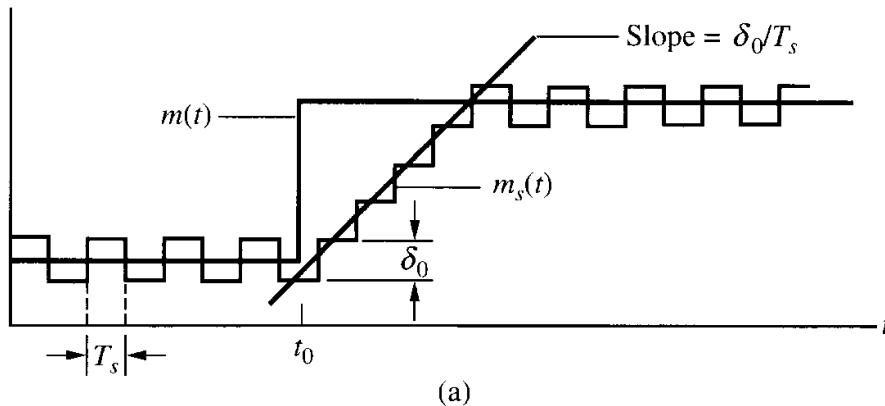
# DM Signal Generation



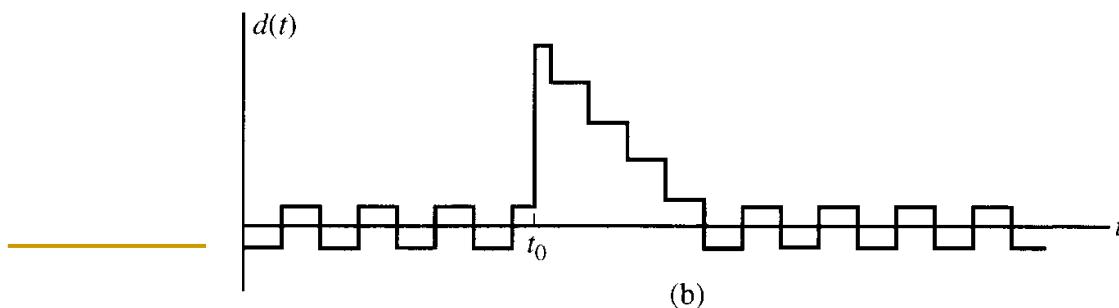
**Figure 3.59**  
Delta modulation. (a) Delta modulator. (b) Modulation waveform and staircase approximation. (c) Modulator output.

# Slope Overload

- The message signal  $m(t)$  has a slope greater than can be followed by the stair-step approximation  $m_s(t)$ .
- Assume step-size =  $\delta_0 \rightarrow$  slope (max) =  $\delta_0/T_s$



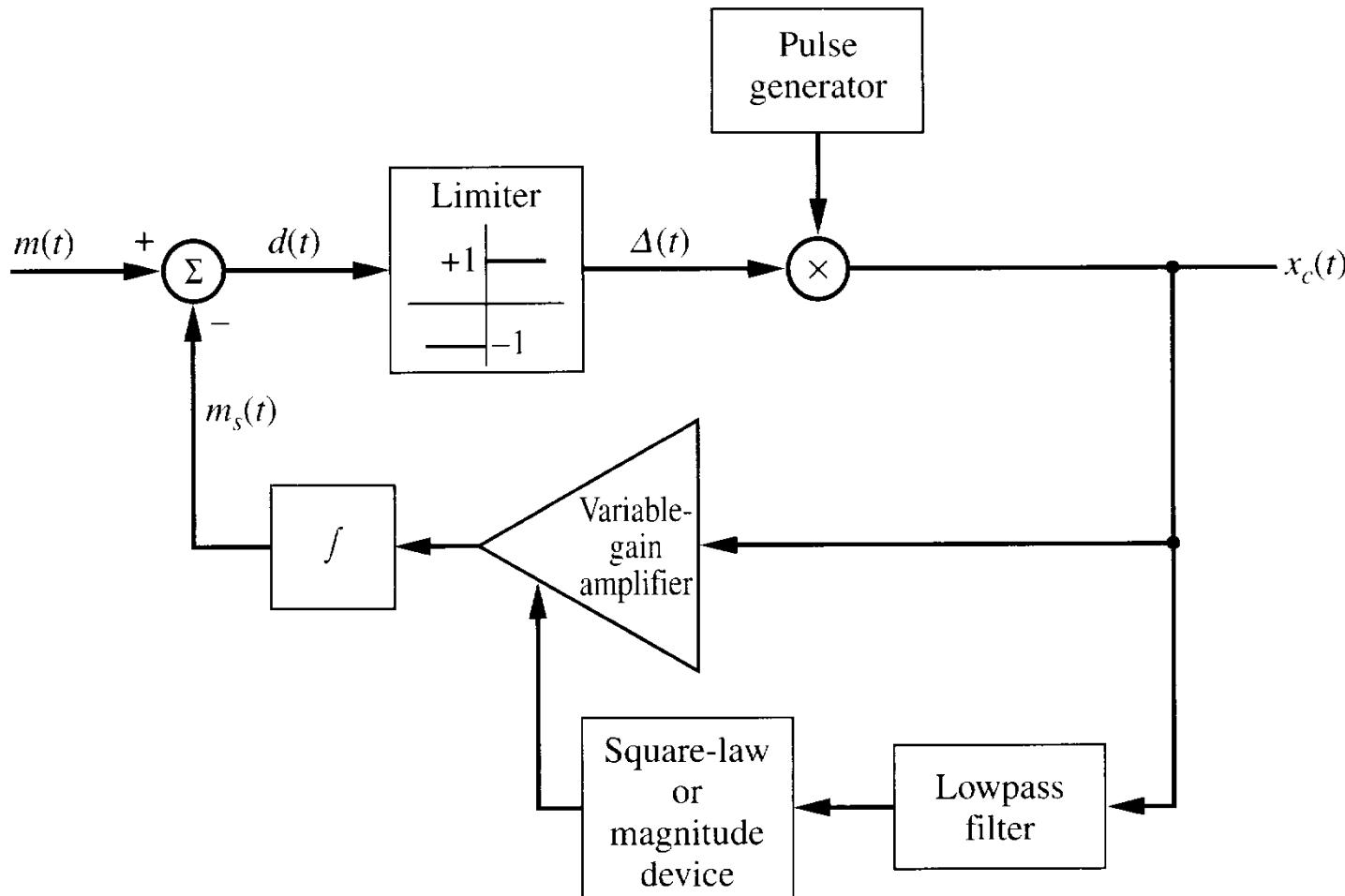
**Figure 3.60**  
Illustration of slope overload.  
(a) Illustration of  $m(t)$  and  $m_s(t)$  with step change in  $m(t)$ . (b) Error between  $m(t)$  and  $m_s(t)$ .



# Solution to Overload

- **Adaptive delta modulation** -- adjust the step-size  $\delta_0$  based on  $x_c(t)$ .
- Idea: If  $m(t) \approx \text{constant}$ ,  $x_c(t)$  alternates in sign  
     $\Rightarrow$  make  $\delta_0 \downarrow$ .  
    If  $m(t) \uparrow$  ( or  $\downarrow$  ) rapidly,  $x_c(t)$  has the same polarity  
     $\Rightarrow$  make  $\delta_0 \uparrow$ .
- Method: Detect the “trend” of signal

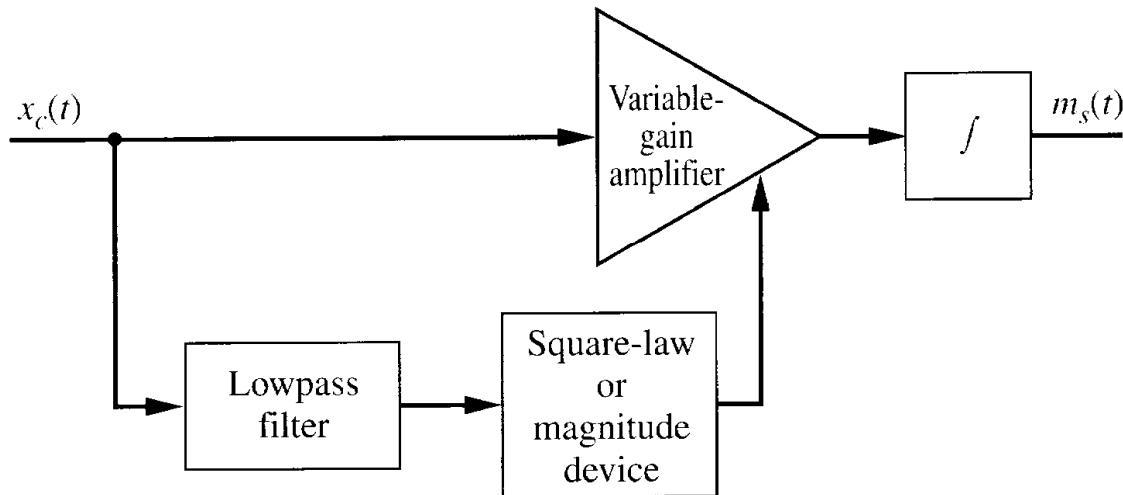
# Adaptive DM



**Figure 3.61**  
Adaptive delta modulator.

# ADM Receiver

- Transmit step-size or regenerate the step-size at the receiver according to pre-decided “rules”.

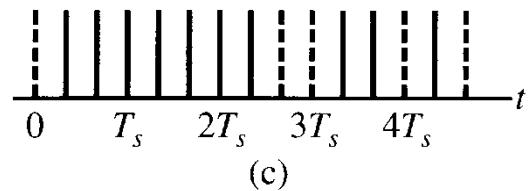
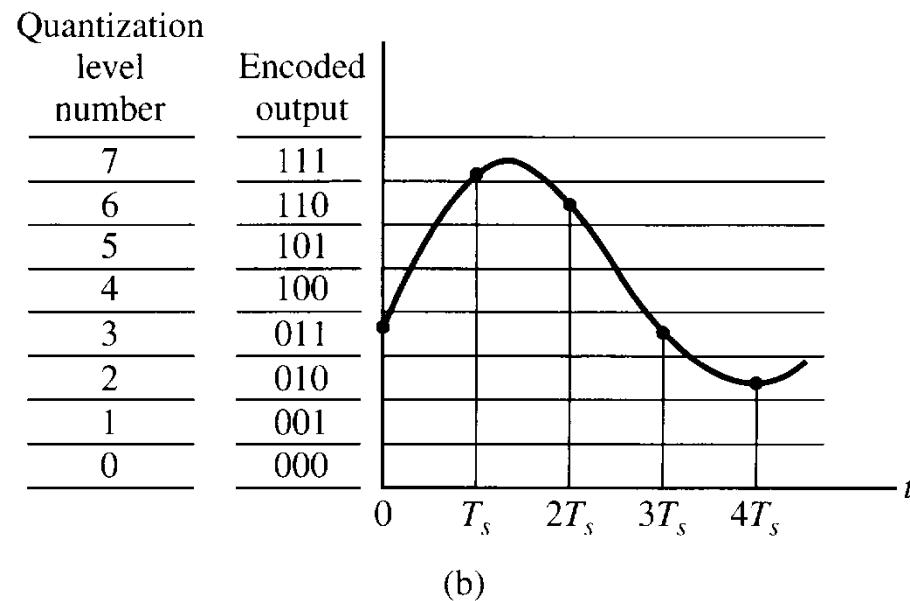
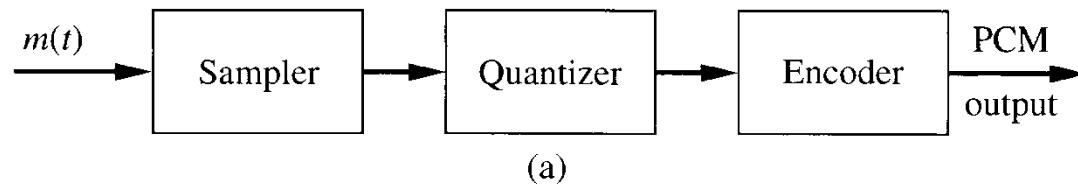


**Figure 3.62**  
Adaptive DM receiver.

# Pulse-Code Modulation (PCM)

- $m(t) \rightarrow$  samples (analog amplitude)  $\rightarrow$  quantized samples  $\rightarrow$  binary representation  $\rightarrow$  binary modulated waveform (ASK (AM), PSK (PM), FSK (FM) **to be discussed in Commun.II** )
- Main advantages of digital communication
  - more reliable communication
- Main disadvantages of digital communication
  - wide BW ( $\leftarrow$ reduced by “compression”)
  - complicated circuits ( $\leftarrow$  cost reduced by VLSI)

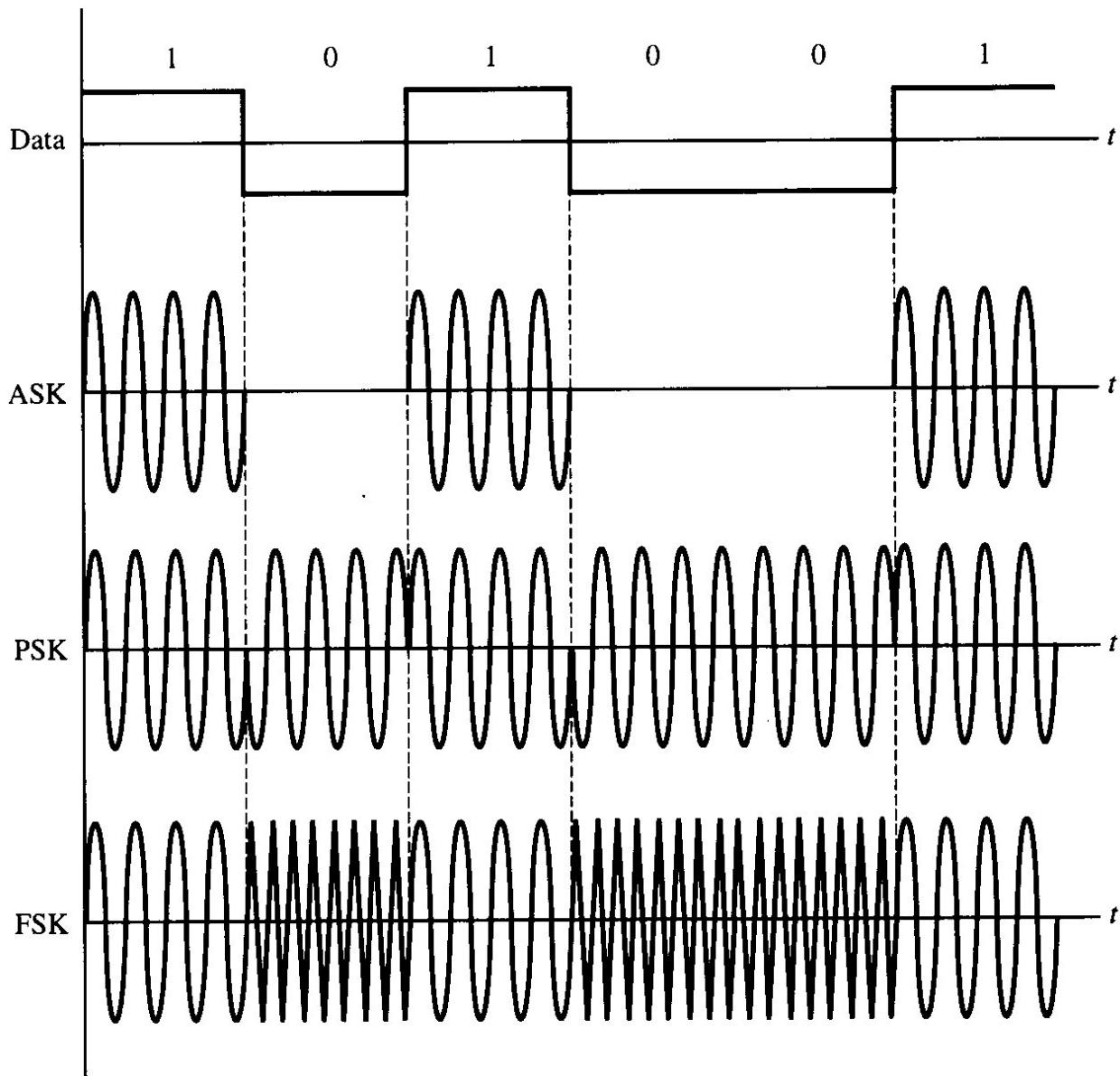
# PCM Signal Generation



**Figure 3.63**  
Generation of PCM. (a) PCM modulator. (b) Quantization and encoding. (c) Transmitted output.

# BW of PCM

- Assume the number of quantization levels =  $q=2^n$   
Message BW =  $W$   
Sampling rate =  $2W$   
 $\Rightarrow 2nW$  binary pulses/second
- Assume maximum width of pulse,  $\Delta\tau = \frac{1}{2nW}$   
 $\Rightarrow$  transmission BW  $\approx knW$ ,  $k=constant$   
Hence,  $B \approx k2W \log_2 q$
- Recovered message error is due to mainly quantization error. Thus,  $q \uparrow \rightarrow \text{error} \downarrow \rightarrow B \uparrow$



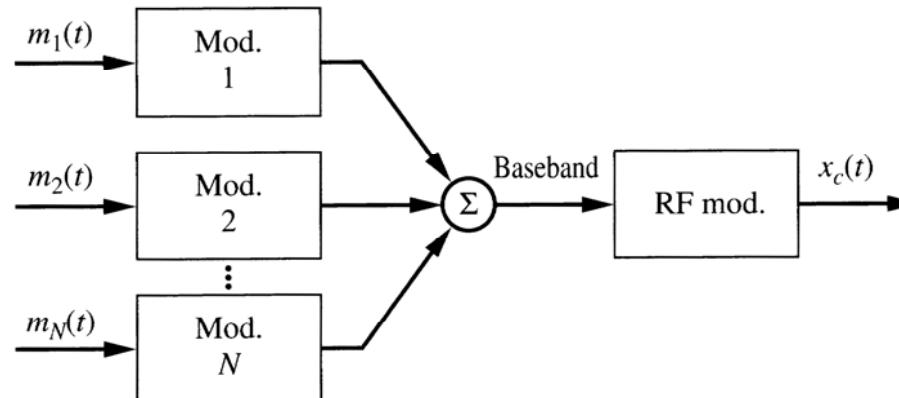
**FIGURE 3.66** An example of digital modulation schemes.

# Multiplexing

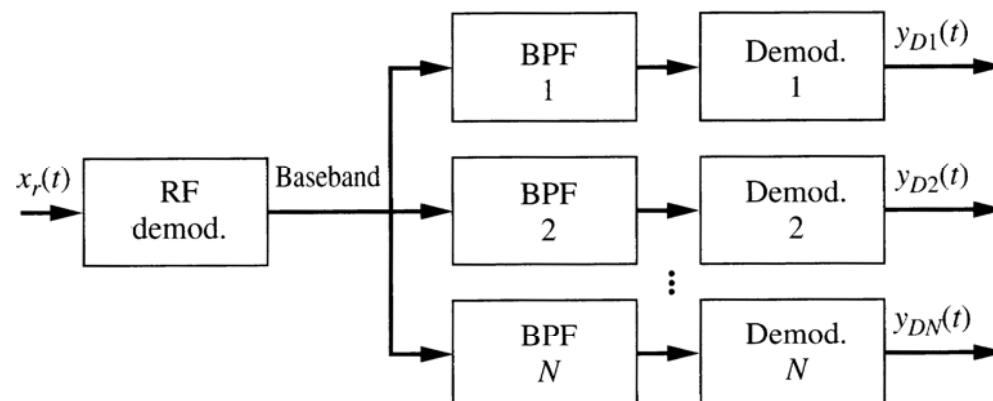
- A number of data sources share the same communication channel.
  - Frequency-Division Multiplexing (FDM)
  - Quadrature Multiplexing (QM)
  - Time-Division Multiplexing (TDM)

# FDM

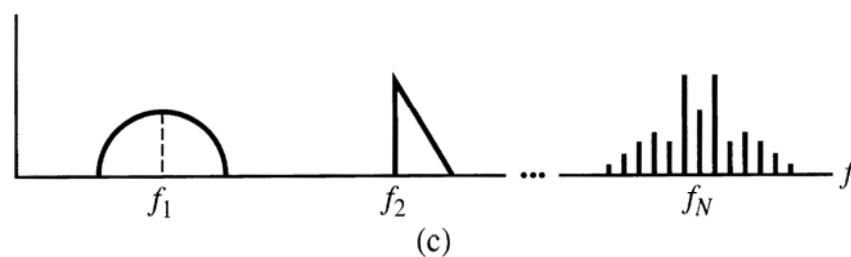
Several message signals are translated, using modulation, to different spectral locations and added to form a baseband signal.



(a)



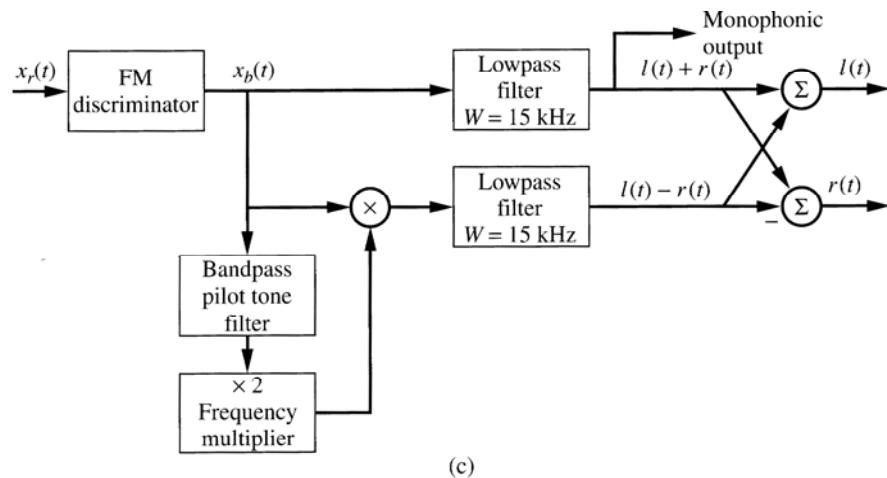
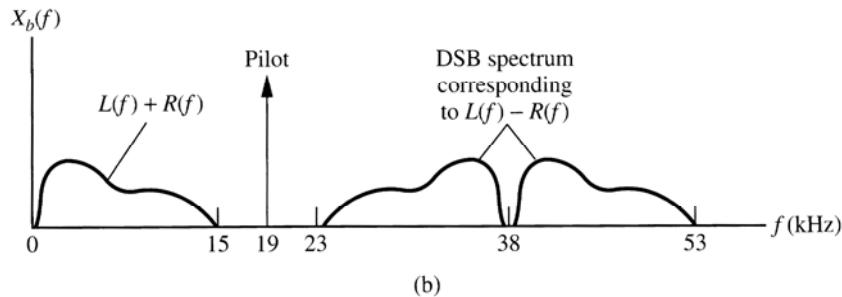
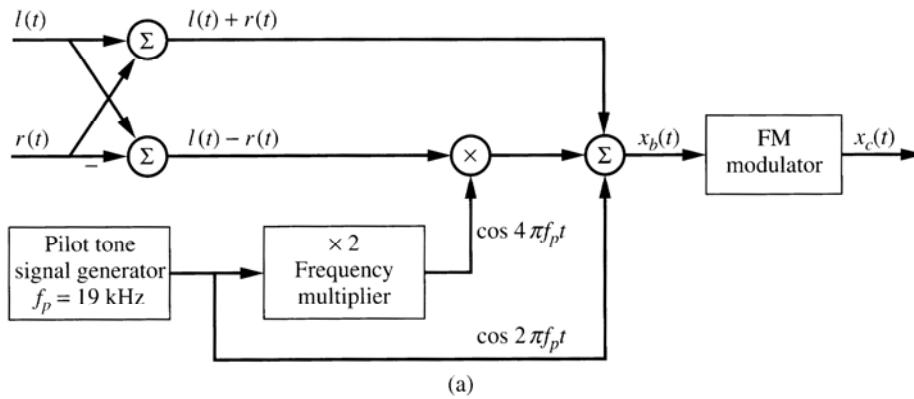
(b)



(c)

**Figure 3.64**  
Frequency-division multiplexing. (a) FDM modulator.  
(b) FDM demodulator.  
(c) Baseband spectrum.

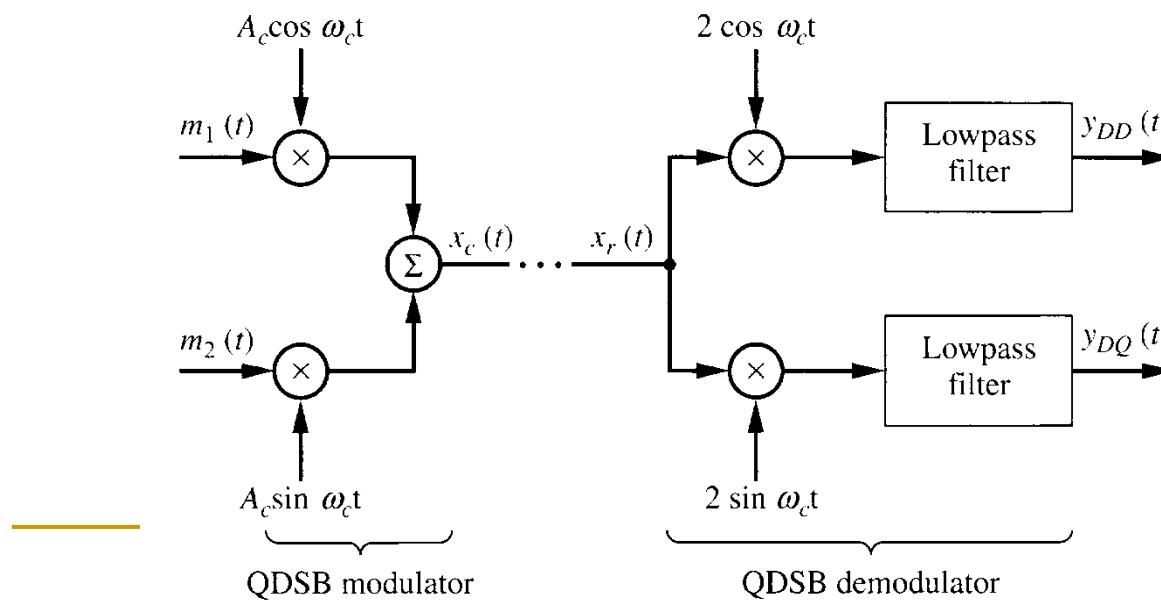
# Example: Stereophonic FM



**Figure 3.65**  
Stereophonic FM transmitter and receiver. (a) Stereophonic FM transmitter. (b) Single-sided spectrum of FM baseband signal. (c) Stereophonic FM receiver.

# Quadrature Multiplexing (QM)

- Quadrature-carrier multiplexing: transmit two signals on the same carrier frequency. (not exactly FDM)
- Note that cos and sin are orthogonal.
- QM → Quadrature Amplitude Modulation (QAM)



**Figure 3.66**  
Quadrature multiplexing.

## <Modulation>

$$x_c(t) = A_C[m_1(t)\cos\omega_c t + m_2(t)\sin\omega_c t].$$

## <Coherent Demodulation>

If the receiver has a carrier phase error, i.e.,

$$LO(t) = 2\cos(\omega_c t + \theta).$$

$$x_r(t) \cdot 2\cos(\omega_c t + \theta)$$

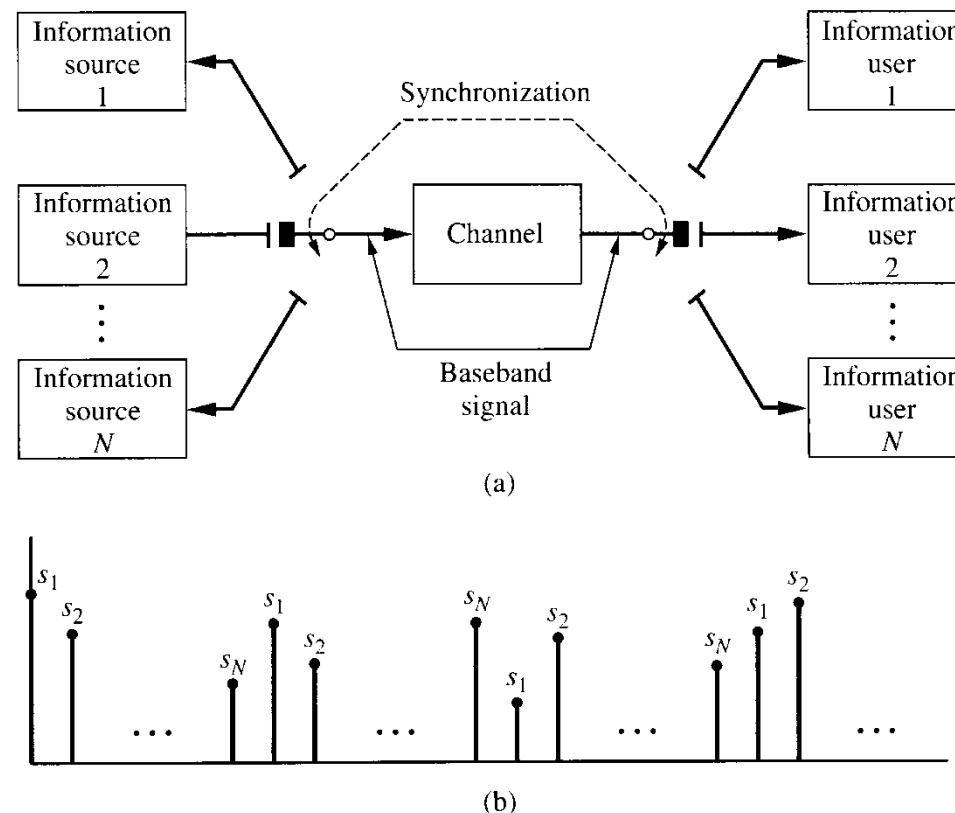
$$= A_C[m_1(t)\cos\theta - m_2(t)\sin\theta]$$

$$+ A_C[m_1(t)\cos(2\omega_c t + \theta) + m_2(t)\sin(2\omega_c t + \theta)].$$

$$\Rightarrow y_{DD}(t) = A_C[m_1(t)\cos\theta - m_2(t)\sin\theta]. \quad (\text{ideal : } \theta \rightarrow 0)$$

# Time-Division Multiplexing (TDM)

- Each message signal occupies a small time slot in every  $T_s$  second.



**Figure 3.67**  
Time-division multiplexing. (a) TDM system. (b) Baseband signal.

# BW of TDM

- A “rough” estimate of BW

Baseband message BW =  $W_i$ . There are  $N$  channels.

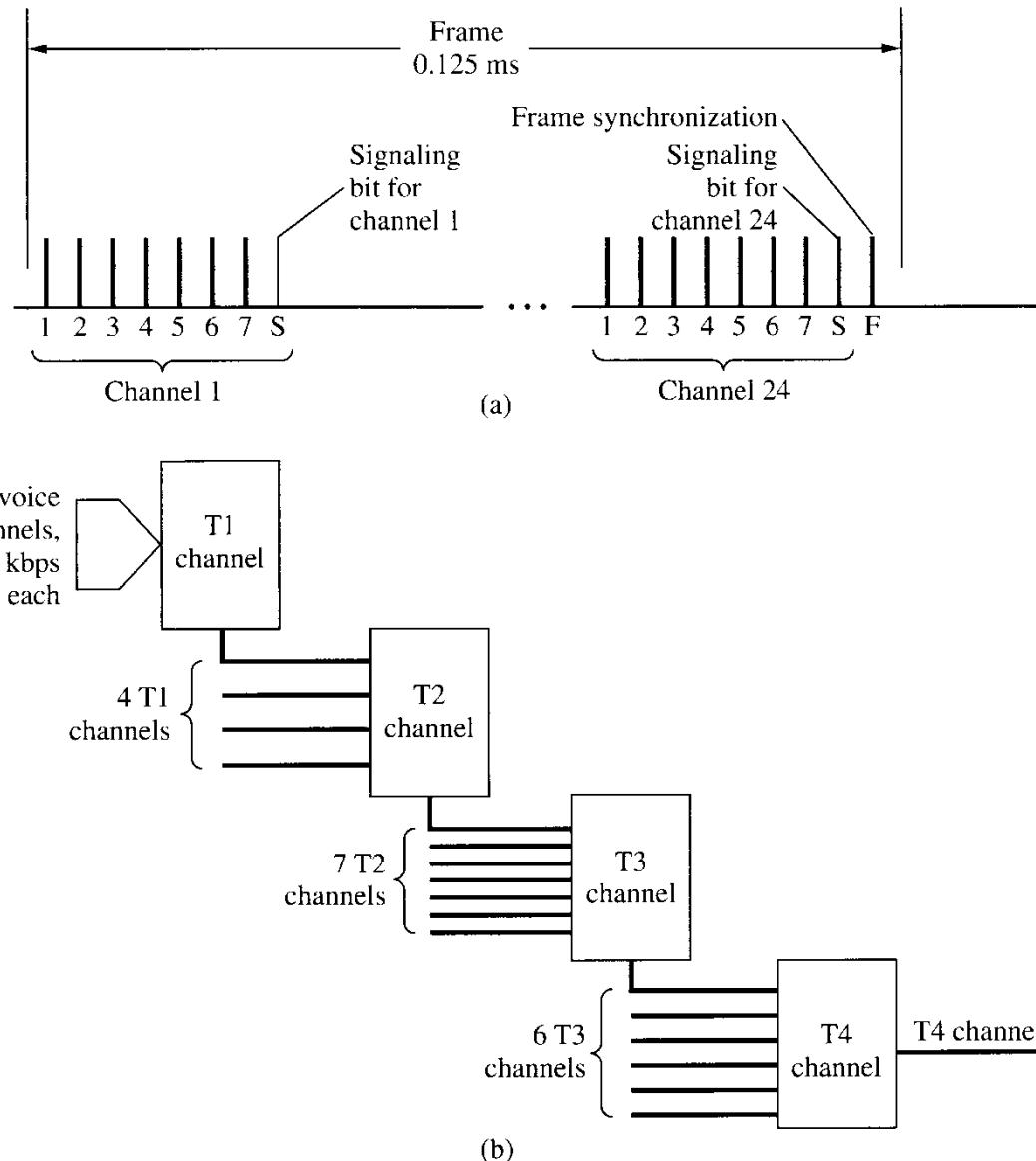
Samples per  $T$  second =  $2W_iT$ .

Total samples per  $T$  second:  $n_s = \sum_{i=1}^N 2W_iT$ . Or,

Total samples per second =  $\sum_{i=1}^N 2W_i$ .

Total baseband BW to accommodate all sources =  $B \square \sum_{i=1}^N W_i$ .

# Example: Digital telephony system



**Figure 3.68**  
Digital multiplexing scheme for digital telephone. (a) T1 frame. (b) Digital multiplexing.

# Comparison of MUX

- **FDM:** simple to implement,  
inter-modulation distortion (crosstalk) due to nonlinear  
channels
- **TDM:** less crosstalk (in memoryless channels),  
difficult to keep synchronization (frame structure, header),  
“digital” (sampled) signals
- **QM:** efficient use of channel, crosstalk between I & Q  
channels (needs coherent demodulation)