

Computer Organization

Reference Solution

HW4

4.2

- 4.2.1** This instruction uses instruction memory, both register read ports, the ALU to add Rd and Rs together, data memory, and write port in Registers.
- 4.2.2** None. This instruction can be implemented using existing blocks.
- 4.2.3** None. This instruction can be implemented without adding new control signals. It only requires changes in the Control logic.
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4.3.1 Clock cycle time is determined by the critical path, which for the given latencies happens to be to get the data value for the load instruction: I-Mem (read instruction), Regs (takes longer than Control), Mux (select ALU input), ALU, Data Memory, and Mux (select value from memory to be written into Registers). The latency of this path is $400 \text{ ps} + 200 \text{ ps} + 30 \text{ ps} + 120 \text{ ps} + 350 \text{ ps} + 30 \text{ ps} = 1130 \text{ ps}$. 1430 ps ($1130 \text{ ps} + 300 \text{ ps}$, ALU is on the critical path).

4.3.2 The speedup comes from changes in clock cycle time and changes to the number of clock cycles we need for the program: We need 5% fewer cycles for a program, but cycle time is 1430 instead of 1130, so we have a speedup of $(1/0.95) \cdot (1130/1430) = 0.83$, which means we actually have a slowdown.

4.3.3 The cost is always the total cost of all components (not just those on the critical path, so the original processor has a cost of I-Mem, Regs, Control, ALU, D-Mem, 2 Add units and 3 Mux units, for a total cost of $1000 + 200 + 500 + 100 + 2000 + 2 \cdot 30 + 3 \cdot 10 = 3890$.

We will compute cost relative to this baseline. The performance relative to this baseline is the speedup we previously computed, and our cost/performance relative to the baseline is as follows:

New Cost: $3890 + 600 = 4490$

Relative Cost: $4490/3890 = 1.15$

Cost/Performance: $1.15/0.83 = 1.39$. We are paying significantly more for significantly worse performance; the cost/performance is a lot worse than with the unmodified processor.

4.4

4.4.1 I-Mem takes longer than the Add unit, so the clock cycle time is equal to the latency of the I-Mem:

200 ps

4.4.2 The critical path for this instruction is through the instruction memory, Sign-extend and Shift-left-2 to get the offset, Add unit to compute the new PC, and Mux to select that value instead of PC+4. Note that the path through the other Add unit is shorter, because the latency of I-Mem is longer than the latency of the Add unit. We have:

$200 \text{ ps} + 15 \text{ ps} + 10 \text{ ps} + 70 \text{ ps} + 20 \text{ ps} = 315 \text{ ps}$

4.4.3 Conditional branches have the same long-latency path that computes the branch address as unconditional branches do. Additionally, they have a long-latency path that goes through Registers, Mux, and ALU to compute the PCSrc condition. The critical path is the longer of the two, and the path through PCSrc is longer for these latencies:

$200 \text{ ps} + 90 \text{ ps} + 20 \text{ ps} + 90 \text{ ps} + 20 \text{ ps} = 420 \text{ ps}$

4.4.4 PC-relative branches.

4.4.5 PC-relative unconditional branch instructions. We saw in part c that this is not on the critical path of conditional branches, and it is only needed for PC-relative branches. Note that MIPS does not have actual unconditional branches (bne zero,zero,Label plays that role so there is no need for unconditional branch opcodes) so for MIPS the answer to this question is actually "None".

4.4.6 Of the two instructions (BNE and ADD), BNE has a longer critical path so it determines the clock cycle time. Note that every path for ADD is shorter than or equal to the corresponding path for BNE, so changes in unit latency will not affect this. As a result, we focus on how the unit's latency affects the critical path of BNE.

This unit is not on the critical path, so the only way for this unit to become critical is to increase its latency until the path for address computation through sign extend, shift left, and branch add becomes longer than the path for PCSrc through registers, Mux, and ALU. The latency of Regs, Mux, and ALU is 200 ps and the latency of Sign-extend, Shift-left-2, and Add is 95 ps, so the latency of Shift-left-2 must be increased by 105 ps or more for it to affect clock cycle time.

4.9

4.9.1

Instruction sequence	Dependences
I1: OR R1, R2, R3	RAW on R1 from I1 to I2 and I3
I2: OR R2, R1, R4	RAW on R2 from I2 to I3
I3: OR R1, R1, R2	WAR on R2 from I1 to I2 WAR on R1 from I2 to I3 WAW on R1 from I1 to I3

4.9.2 In the basic five-stage pipeline WAR and WAW dependences do not cause any hazards. Without forwarding, any RAW dependence between an instruction and the next two instructions (if register read happens in the second half of the clock cycle and the register write happens in the first half). The code that eliminates these hazards by inserting NOP instructions is:

Instruction sequence	
OR R1, R2, R3	Delay I2 to avoid RAW hazard on R1 from I1
NOP	
NOP	Delay I3 to avoid RAW hazard on R2 from I2
OR R2, R1, R4	
NOP	
NOP	
OR R1, R1, R2	

4.9.3 With full forwarding, an ALU instruction can forward a value to EX stage of the next instruction without a hazard. However, a load cannot forward to the EX stage of the next instruction (by can to the instruction after that). The code that eliminates these hazards by inserting NOP instructions is:

Instruction sequence	
OR R1, R2, R3	No RAW hazard on R1 from I1 (forwarded)
OR R2, R1, R4	
OR R1, R1, R2	No RAW hazard on R2 from I2 (forwarded)

4.9.4 The total execution time is the clock cycle time times the number of cycles. Without any stalls, a three-instruction sequence executes in 7 cycles (5 to complete the first instruction, then one per instruction). The execution without forwarding must add a stall for every NOP we had in 4.9.2, and execution forwarding must add a stall cycle for every NOP we had in 4.9.3. Overall, we get:

No forwarding	With forwarding	Speedup due to forwarding
$(7+4)*250=2750$	$(7+4)*300=2100$	$2750/2100=1.31$

4.9.5 With ALU-ALU-only forwarding, an ALU instruction can forward to the next instruction, but not to the second-next instruction (because that would be forwarding from MEM to EX). A load cannot forward at all, because it determines the data value in MEM stage, when it is too late for ALU-ALU forwarding. We have:

Instruction sequence	
OR R1, R2, R3	
OR R2, R1, R4	ALU-ALU forwarding of R1 from I1
OR R1, R1, R2	ALU-ALU forwarding of R2 from I2

4.9.6

No forwarding	With ALU-ALU forwarding only	Speedup with ALU-ALU forwarding
$(7+4)*250=2750$	$(7)*290=2030$	$2750/2030=1.35$

4.10

4.10.1 In the pipelined execution shown below, *** represents a stall when an instruction cannot be fetched because a load or store instruction is using the memory in that cycle. Cycles are represented from left to right, and for each instruction we show the pipeline stage it is in during that cycle:

Instruction	Pipeline Stage	Cycles
SW R16, 12(R6)	IF ID EX MEM WB	11
LW R16, 8(R6)	IF ED EX MEM WB	
BEQ R5, R4, Lb1	IF ID EX MEM WB	
ADD R5, R1, R4	*** ** IF ID EX MEM WB	
SLT R5, R15, R4	IF ID EX MEM WB	

We can not add NOPs to the code to eliminate this hazard – NOPs need to be fetched just like any other instructions, so this hazard must be addressed with a hardware hazard detection unit in the processor.

4.10.2 This change only saves one cycle in an entire execution without data hazards (such as the one given). This cycle is saved because the last instruction finishes one cycle earlier (one less stage to go through). If there were data hazards from loads to other instructions, the change would help eliminate some stall cycles.

Instructions Executed	Cycles with 5 stages	Cycles with 4 stages	Speedup
5	$4 + 5 = 9$	$3 + 5 = 8$	$9/8 = 1.13$

4.10.3 Stall-on-branch delays the fetch of the next instruction until the branch is executed. When branches execute in the EXE stage, each branch causes two stall cycles. When branches execute in the ID stage, each branch only causes one stall cycle. Without branch stalls (e.g., with perfect branch prediction) there are no stalls, and the execution time is 4 plus the number of executed instructions. We have:

Instructions Executed	Branches Executed	Cycles with branch in EXE	Cycles with branch in ID	Speedup
5	1	$4 + 5 + 1*2 = 11$	$4 + 5 + 1*1 = 10$	$11/10 = 1.10$

4.10.4 The number of cycles for the (normal) 5-stage and the (combined EX/MEM) 4-stage pipeline is already computed in 4.10.2. The clock cycle time is equal to the latency of the longest-latency stage. Combining EX and MEM stages affects clock time only if the combined EX/MEM stage becomes the longest-latency stage:

Cycle time with 5 stages	Cycle time with 4 stages	Speedup
200 ps (IF)	210 ps (MEM + 20 ps)	$(9*200)/(8*210) = 1.07$

4.10.5

New ID latency	New EX latency	New cycle time	Old cycle time	Speedup
180 ps	140 ps	200 ps (IF)	200 ps (IF)	$(11*200)/(10*200) = 1.10$

4.10.6 The cycle time remains unchanged: a 20 ps reduction in EX latency has no effect on clock cycle time because EX is not the longest-latency stage. The change does affect execution time because it adds one additional stall cycle to each branch. Because the clock cycle time does not improve but the number of cycles increases, the speedup from this change will be below 1 (a slowdown). In 4.10.3 we already computed the number of cycles when branch is in EX stage. We have:

	Cycles with branch in EX	Execution time (branch in EX)	Cycles with branch in MEM	Execution time (branch in MEM)	Speedup
a.	$4 + 5 + 1*2 = 11$	$11*200 \text{ ps} = 2200 \text{ ps}$	$4 + 5 + 1*3 = 12$	$12*200 \text{ ps} = 2400 \text{ ps}$	0.92

4.13

4.13.1

```
ADD R5,R2,R1
NOP
NOP
LW R3,4(R5)
LW R2,0(R2)
NOP
OR R3,R5,R3
NOP
NOP
SW R3,0(R5)
```

4.13.2 We can move up an instruction by swapping its place with another instruction that has no dependences with it, so we can try to fill some NOP slots with such instructions. We can also use R7 to eliminate WAW or WAR dependences so we can have more instructions to move up.

I1: ADD R5,R2,R1	
I3: LW R2,0(R2)	Moved up to fill NOP slot
NOP	
I2: LW R3,4(R5)	
NOP	
NOP	Had to add another NOP here, so there is no performance gain
I4: OR R3,R5,R3	
NOP	
NOP	
I5: SW R3,0(R5)	

4.13.3 With forwarding, the hazard detection unit is still needed because it must insert a one-cycle stall whenever the load supplies a value to the instruction that immediately follows that load. Without the hazard detection unit, the instruction that depends on the immediately preceding load gets the stale value the register had before the load instruction.

Code executes correctly (for both loads, there is no RAW dependence between the load and the next instruction).

4.13.4 The outputs of the hazard detection unit are PCWrite, IF/IDWrite, and ID/EXZero (which controls the Mux after the output of the Control unit). Note that IF/IDWrite is always equal to PCWrite, and ED/ExZero is always the opposite of PCWrite. As a result, we will only show the value of PCWrite for each cycle. The outputs of the forwarding unit is ALUin1 and ALUin2, which control Muxes that select the first and second input of the ALU. The three possible values for ALUin1 or ALUin2 are 0 (no forwarding), 1 (forward ALU output from previous instruction), or 2 (forward data value for second-previous instruction). We have:

Instruction sequence	First five cycles					Signals
	1	2	3	4	5	
ADD R5,R2,R1	IF	ID	EX	MEM	WB	1: PCWrite=1, ALUin1=X, ALUin2=X
LW R3,4(R5)		IF	ID	EX	MEM	2: PCWrite=1, ALUin1=X, ALUin2=X
LW R2,0(R2)			IF	ID	EX	3: PCWrite=1, ALUin1=0, ALUin2=0
OR R3,R5,R3				IF	ID	4: PCWrite=1, ALUin1=1, ALUin2=0
SW R3,0(R5)					IF	5: PCWrite=1, ALUin1=0, ALUin2=0

4.13.5 The instruction that is currently in the ID stage needs to be stalled if it depends on a value produced by the instruction in the EX or the instruction in the MEM stage. So we need to check the destination register of these two instructions. For the instruction in the EX stage, we need to check Rd for R-type instructions and Rd for loads. For the instruction in the MEM stage, the destination register is already selected (by the Mux in the EX stage) so we need to check that register number (this is the bottommost output of the EX/MEM pipeline register). The additional inputs to the hazard detection unit

are register Rd from the ID/EX pipeline register and the output number of the output register from the EX/MEM pipeline register. The Rt field from the ID/EX register is already an input of the hazard detection unit in Figure 4.60.

No additional outputs are needed. We can stall the pipeline using the three output signals that we already have.

4.13.6 As explained for part e, we only need to specify the value of the PCWrite signal, because IF/IDWrite is equal to PCWrite and the ID/EXzero signal is its opposite. We have:

Instruction sequence	First five cycles					Signals
	1	2	3	4	5	
ADD R5,R2,R1	IF	ID	EX	MEM	WB	1: PCWrite=1
LW R3,4(R5)		IF	ID	***	***	2: PCWrite=1
LW R2,0(R2)			IF	***	***	3: PCWrite=1
OR R3,R5,R3					***	4: PCWrite=0
SW R3,0(R5)						5: PCWrite=0

4.14

4.14.1

Executed Instructions	Pipeline Cycles													
	1	2	3	4	5	6	7	8	9	10	11	12	13	14
LW R2,0(R1)	IF	ID	EX	MEM	WB									
BEQ R2,R0,Label2 (NT)		IF	ID	***	EX	MEM	WB							
LW R3,0(R2)						IF	ID	EX	MEM	WB				
BEQ R3,R0,Label1 (T)							IF	ID	***	EX	MEM	WB		
BEQ R2,R0,Label2 (T)								IF	***	ID	EX	MEM	WB	
SW R1,0(R2)										IF	ID	EX	MEM	WB

4.14.2

Executed Instructions	Pipeline Cycles													
	1	2	3	4	5	6	7	8	9	10	11	12	13	14
LW R2,0(R1)	IF	ID	EX	MEM	WB									
BEQ R2,R0,Label2 (NT)		IF	ID	***	EX	MEM	WB							
LW R3,0(R2)			IF	***	ID	EX	MEM	WB						
BEQ R3,R0,Label1 (T)						IF	ID	EX	MEM	WB				
ADD R1,R3,R1							IF	ID	EX	MEM	WB			
BEQ R2,R0,Label2 (T)								IF	ID	EX	MEM	WB		
LW R3,0(R2)									IF	ID	EX	MEM	WB	
SW R1,0(R2)										IF	ID	EX	MEM	WB

4.14.3

LW R2,0(R1)
Label1: BEZ R2,Label2 ; Not taken once, then taken
LW R3,0(R2)
BEZ R3,Label1 ; Taken
ADD R1,R3,R1
Label2: SW R1,0(R2)

4.14.4 The hazard detection logic must detect situations when the branch depends on the result of the previous R-type instruction, or on the result of two previous loads. When the branch uses the values of its register operands in its ID stage, the R-type instruction's result is still being generated in the EX stage. Thus we must stall the processor and repeat the ID stage of the branch in the next cycle. Similarly, if the branch depends on a load that immediately precedes it, the result of the load is only generated two cycles after the branch enters the ID stage, so we must stall the branch for two cycles. Finally, if the branch depends on a load that is the second-previous instruction, the load is completing its MEM stage when the branch is in its ID stage, so we must stall the branch for one cycle. In all three cases, the hazard is a data hazard.

Note that in all three cases we assume that the values of preceding instructions are forwarded to the ID stage of the branch if possible.

4.14.5 For part a we have already shows the pipeline execution diagram for the case when branches are executed in the EX stage. The following is the pipeline diagram when branches are executed in the ID stage, including new stalls due to data dependences described for part d:

Executed Instructions	Pipeline Cycles														
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
LW R2,0(R1)	IF	ID	EX	MEM	WB										
BEQ R2,R0,Label12 (NT)		IF	***	***	ID	EX	MEM	WB							
LW R3,0(R2)						IF	ID	EX	MEM	WB					
BEQ R3,R0,Label11 (T)							IF	***	***	ID	EX	MEM	WB		
BEQ R2,R0,Label12 (T)										IF	ID	EX	MEM	WB	
SW R1,0(R2)											IF	ID	EX	MEM	WB

Now the speedup can be computed as:

$$14/15 = 0.93$$

4.14.6 Branch instructions are now executed in the ID stage. If the branch instruction is using a register value produced by the immediately preceding instruction, as we described for part d the branch must be stalled because the preceding instruction is in the EX stage when the branch is already using the stale register values in the ID stage. If the branch in the ID stage depends on an R-type instruction that is in the MEM stage, we need forwarding to ensure correct execution of the branch. Similarly, if the branch in the ID stage depends on an R-type of load instruction in the WB stage, we need forwarding to ensure correct execution of the branch. Overall, we need another forwarding unit that takes the same inputs as the one that forwards to the EX stage. The new forwarding unit should control two Muxes placed right before the branch comparator. Each Mux selects between the value read from Registers, the ALU output from the EX/MEM pipeline register, and the data value from the MEM/WB pipeline register. The complexity of the new forwarding unit is the same as the complexity of the existing one.

4.15

4.15.1 Each branch that is not correctly predicted by the always-taken predictor will cause 3 stall cycles, so we have:

Extra CPI
$3*(1 - 0.45)*0.25 = 0.41$

4.15.2 Each branch that is not correctly predicted by the always-not-taken predictor will cause 3 stall cycles, so we have:

Extra CPI
$3*(1 - 0.55)*0.25 = 0.34$

4.15.3 Each branch that is not correctly predicted by the 2-bit predictor will cause 3 stall cycles, so we have:

Extra CPI
$3*(1 - 0.85)*0.25 = 0.113$

4.15.4 Correctly predicted branches had CPI of 1 and now they become ALU instructions whose CPI is also 1. Incorrectly predicted instructions that are converted also become ALU instructions with a CPI of 1, so we have:

CPI without conversion	CPI with conversion	Speedup from conversion
$1 + 3*(1-0.85)*0.25 = 1.113$	$1 + 3*(1-0.85)*0.25*0.5 = 1.056$	$1.113/1.056 = 1.054$

4.15.5 Every converted branch instruction now takes an extra cycle to execute, so we have:

CPI without conversion	Cycles per original instruction with conversion	Speedup from conversion
1.113	$1 + (1 + 3*(1 - 0.85))*0.25*0.5 = 1.181$	$1.113/1.181 = 0.94$

4.15.6 Let the total number of branch instructions executed in the program be B. Then we have:

Correctly predicted	Correctly predicted non-loop-back	Accuracy on non-loop-back branches
$B*0.85$	$B*0.05$	$(B*0.05)/(B*0.20) = 0.25$ (25%)

